# Analysis of the Optical Response Characteristics of the TFT-LCD

Yoshinori NUMANO, Masahiro HAYAMA, and Teruhiko YAMAZAKI

Materials & Electronic Devices Laboratory, Mitsubishi Electric Corporation, Amagasaki, Hyougo 661, Japan

A model, which takes into account the time dependence and voltage dependence of the dielectric constant of liquid crystal by using an equivalent circuit, is proposed to analyze the optical response characteristics of the TFT addressed LCD (TFT-LCD). The 30Hz flicker, which appears in the optical rise state of the TFT-LCD, can be calculated and analyzed numerically. The parameter  $M_{30}$ , which indicates the normalized amplitude of the 30Hz flicker, is reduced by increasing the storage capacitance (C<sub>ST</sub>).  $M_{30}$  begins to saturate at C<sub>ST</sub>=0.5pF.  $M_{30}$  is lower than 0.055 and the change in V<sub>COM</sub> for minimizing  $M_{30}$  is +0.1V at C<sub>ST</sub>=0.5pF.

## 1.Introduction

Recently, the development of TFT-LCDs has been accelerated<sup>1)</sup>, because of their high image quality in comparison with direct multiplexing LCDs. However, since the TFT-LCD is not operated in ideal static drive, the problem of the 30Hz flicker, especially in gray scale operation, still remains. We analyzed the optical response characteristics of the TFT-LCD numerically in order to investigate the 30Hz flicker. Several models have been proposed to calculate the optical response characteristics of the  $TFT-LCD^{2})-4$ ). We employed an equivalent circuit model because it is suitable for a large amount of calculation at high speed. Previously, an analysis using an equivalent circuit model showed that the asymmetric voltage in the LC caused the 30Hz flicker<sup>4</sup>). However, it could not calculate the optical response characteristics of the TFT-LCD directly because it did not consider the time dependence of the dielectric constant of the TN-LC cell ( $\varepsilon$  LC).

In this paper, we present the calculation method of the optical response characteristics of the TFT-LCD taking the time depenence and voltage dependence of  $\varepsilon_{LC}$  into account by using an equivalent circuit model. Then, the calculated results of the optical response characteristics of the TN-LC cell are compared with measurements. We analyze the 30Hz flicker which appears in the optical rise state of the TFT-LCD due to the gate-drain coupling capacitance  $(C_{gd})$  and the change in LC capacitance  $(C_{L,C})^{5}$ .

#### 2.Method of Calculation

Figure 1 shows a pixel equivalent circuit of the TFT-LCD. The following differential equation eq.(1) is obtained from this equivalent circuit and solved numerically:

$$\begin{bmatrix} c_{X} & -c_{SiN} & 0 & 0 \\ -c_{SiN} & c_{SiN} + c_{PI} & -c_{PI} & 0 \\ 0 & -c_{PI} & c_{PI} + c_{LC} (v_{LC}(t), t) & -c_{LC} (v_{LC}(t), t) \\ 0 & 0 & -c_{LC} (v_{LC}(t), t) & c_{LC} (v_{LC}(t), t) + c_{PI} \end{bmatrix}$$

$$\times \begin{bmatrix} \dot{v}_{1} \\ \dot{v}_{2} \\ \dot{v}_{3} \\ \dot{v}_{4} \end{bmatrix} = \begin{bmatrix} c_{gd} \cdot \dot{v}_{g} + c_{ds} \cdot \dot{v}_{S} - \frac{v_{1} - v_{2}}{R_{SiN}} - \frac{v_{1} - v_{ST}}{R_{ST}} + I_{dS} \\ \frac{v_{1} - v_{2}}{R_{SiN}} - \frac{v_{2} - v_{3}}{R_{PI}} \\ \frac{v_{2} - v_{3}}{R_{PI}} - \frac{v_{3} - v_{4}}{R_{LC}} \\ \frac{v_{3} - v_{4}}{R_{LC}} - \frac{v_{4} - v_{COM}}{R_{PI}} \end{bmatrix} , (1)$$

$$V = dV / dt ,$$
(3)

$$c_{\text{LC}}(v_{\text{LC}}(t), t) = \varepsilon_0 \cdot \varepsilon_{\text{LC}}(v_{\text{LC}}(t), t) \cdot S_{\text{PIXEL}} \wedge d_{\text{LC}} , \quad (4)$$

$$V_{\rm LC}(t) = V_3 - V_4 \quad , \tag{5}$$



Fig.1 A pixel equivalent circuit.

where  $\varepsilon_{LC}$  is the dielectric constant of the TN-LC cell,  $I_{ds}$  is the drain current of the TFT, and  $S_{PIXEL}$  is the area of a pixel.

The capacitance of the TN-LC cell ( $C_{LC}$ ) depends on time and voltage due to the dielectric anisotropy of the LC. We introduce eq.(3) to express the time dependence and voltage dependence of  $C_{LC}$ . The voltage dependence of  $\varepsilon_{LC}$  is given by the measurement of the capacitance voltage characteristics of the TN-LC cell. The time dependence of  $\varepsilon_{LC}$ are expressed by introducing the time dependence of orientation vector of the LC have a relaxation phenomenon to the change of applied voltage, as follows:

$$\varepsilon_{\mathrm{LC}}(\mathbb{V}_{\mathrm{LC}}(\mathbf{t}_{0}), \mathbf{t}_{0} + \Delta \mathbf{t}) - \varepsilon_{\mathrm{LC}}(\mathbb{V}_{\mathrm{LC}}(\mathbf{t}_{0}), \mathbf{t}_{0}) = \\ \{\varepsilon_{\mathrm{LC}}(\mathbb{V}_{\mathrm{LC}}(\mathbf{t}_{0}), \infty) - \varepsilon_{\mathrm{LC}}(\mathbb{V}_{\mathrm{LC}}(\mathbf{t}_{0}), \mathbf{t}_{0})\} \\ \times \{1 - \exp(-\mathbf{k} \cdot \Delta \mathbf{t} \neq \tau)\}, \tag{6}$$

where  $\tau$  is the relaxation time,

 $\varepsilon_{LC}(V_{LC}(t_0), t_0)$  is the dielectric constant at t=t<sub>0</sub> with  $V_{LC}(t_0)$ .  $\varepsilon_{LC}(V_{LC}(t_0), \infty)$  is the dielectric constant in the steady state



Fig.2 Transmission-Voltage characteristics (solid line) and Dielectric Constant-Voltage characteristics (dashed line) of the TN-LC cell.



Fig.3 Response time of the transmisson as a function of drive voltage of the TN-LC cell: O is measured  $\tau_{\rm ON}$ ,  $\Delta$  is measured  $\tau_{\rm OFF}$ , solid line is calculated  $\tau_{\rm ON}$  using eq.(7).

with  $V_{LC}(t_0)$ .  $\varepsilon_{LC}(V_{LC}(t_0), \infty)$  is obtained from the measured voltage dependence of  $\varepsilon_{LC}$ of the TN-LC cell. Since the dielectric constant and the transmission of the TN-LC cell correspond 1 to 1, we assume that the relaxation time of  $\varepsilon_{LC}$  is equivalent to the response time of the transmission. Then, the following equations obtained from the continuum theory<sup>6</sup>) are used:

en 
$$\varepsilon_{\mathrm{LC}}(\mathbb{V}_{\mathrm{LC}}(\mathbf{t}_{0}), \mathbf{t}_{0}) \leq \varepsilon_{\mathrm{LC}}(\mathbb{V}_{\mathrm{LC}}(\mathbf{t}_{0}), \infty),$$
  
$$\tau = \tau_{0N} \infty \frac{\eta \cdot \mathrm{d}_{\mathrm{LC}}^{2}}{\varepsilon_{0} \cdot \varDelta \varepsilon \cdot \mathbb{V}_{\mathrm{LC}}(\mathbf{t}_{0})^{2} - \pi^{2} \cdot \mathbb{K}_{\mathrm{II}}}, \quad (7)$$

where  $\Delta \varepsilon = \varepsilon / / - \varepsilon \bot$ ,

wh

when 
$$\varepsilon_{LC}(V_{LC}(t_0), t_0) > \varepsilon_{LC}(V_{LC}(t_0), \infty),$$
  
 $\tau = \tau_{0FF} = \text{constant},$  (8)

where  $\eta$  is the coefficient of viscosity,  $K_{11}$  is the elastic constant.  $\tau_{ON}$  is the time required from the time when the voltage is applied to the time when the transmission reaches 90% of its final value.  $\tau_{OFF}$  is the time required from the time when the applied voltage becomes 0 V to the time when the transmission reaches 10% of its maximum value.

The characteristics of the TN-LC cell are measured to obtain the parameters for the calculation. The voltage dependence of  $\varepsilon_{\rm LC}$ and transmission-voltage characteristics of the TN-LC cell are measured as shown in Fig.2. Figure 3 shows the response time of the transmission as a function of voltage. The calculated  $\tau_{\rm ON}$  using eq.(7) is also shown in Fig.3.  $\tau_{\rm OFF}$  is 20ms.

988

Current-voltage characteristics of the TFT are calculated by using the gradualchannel approximation<sup>7)</sup>. The drain current in the off state is assumed to be proportional to the voltage between  $V_S$  and  $V_1$ , independent on  $V_G$ .

### 3.Results and Discussion

At first, we confirm that the calculation of the optical response characteristics of the TN-LC cell without TFT is possible using the above method. The optical response characteristics of the TN-LC cell are calculated and compared with the measurement. The TN-LC cell is driven by the static drive with amplitude voltage  $riangle V_S$ . Figure 4 shows the measured and calculated optical rise characteristics of the TN-LC cell. The measured and calculated optical fall characteristics of the TN-LC cell are shown in Fig.5. The calculated results are in agreement with the measured results. From these results, the optical response characteristics of the TN-LC cell can be calculated by using an equivalent circuit model in consideration of the voltage dependence and time dependence of ELC.

We numerically analyze the 30Hz flicker which appears in the optical rise state of the TFT-LCD due to  $\ensuremath{\mathsf{Cgd}}$  and the change in  $C_{LC}^{5}$ ).  $C_{gd}$  and  $C_{ds}$  are 0.04pF and 0.02pF in the calculation. The TFT-LCD of 640(H)X240(V) pixels is driven by the frame inversion of the non-interlace method with the frame frequency of 60Hz. Figure 6 shows the input signal which is applied to a pixel. In the calculation,  $riangle V_S$  which produces the transmission of 0% is applied initially.  $riangle V_S$  is changed after voltages V1, V2, V3, and V4 reach the steady state. When the gate signal becomes  $V_G(ON)$  for the first time after  $riangle V_S$ is changed, the time is defined as t=0. The parameter M<sub>30</sub> is defined to evaluate the 30Hz flicker, shown as follows:

 $\label{eq:m30} \begin{array}{ll} {}^{M_{30}} = {}^{F_{30}/T_m} \qquad \qquad (9) \\ \mbox{where } {}^{F_{30}} \mbox{ is the amplitude of the 30Hz component of the calculated result and } {}^{T_m} \mbox{ is the mean transmission in a frame.} \end{array}$ 

Figure 7 shows  $M_{30}$  as a function of the change in  $V_{COM}$  ( $\bigtriangleup\,V_{COM})$  without a storage capacitor.  $\bigtriangleup\,V_S$  of 3.7V and 5.0V are the



Fig.4 Measured(solid line) and calculated (dashed line) optical rise characteristics of the TN-LC cell.



Fig.5 Measured(solid line) and calculated (dashed line) optical fall characteristics of the TN-LC cell.



Fig.6 Input signal wave form  $V_G(ON)=20V$ ,  $V_G(OFF)=-5V$ ,  $V_{SCOM}=10V$ ,  $V_{COM}=4V$ 

voltages which produce the transmission of 10% and 90%.  $\triangle V_{COM}$  for minimizing  $M_{30}$  at  $\triangle V_S=3.7V$  is +1.05V, and that at  $\triangle V_S=5.0V$  is +1.60V.  $\triangle V_{COM}$  for minimizing  $M_{30}$  varies depending on  $\triangle V_S$ . This is because the drain voltage shift through  $C_{gd}$  ( $\triangle V_{gd}$ ) varies due to the change of  $C_{LC}$  with  $\triangle V_S$ . Therefore, the 30Hz flicker can be minimized by adjusting  $V_{COM}$  in response to the  $\triangle V_{gd}$  changes.

The optical rise characteristics of the

TFT-LCD with storage capacitor is calculated. Figure 8 shows M<sub>30</sub> as a function of  $C_{gd}/(C_{ST}+C_{LCm})$ . T<sub>10</sub>, T<sub>50</sub>, and T<sub>90</sub> represent the source signal amplitude which produce the transmission of 10%, 50%, and 90%, respectively. C<sub>LCm</sub> is the mean capacitance of  $\mathrm{C}_{LC}$  during a frame.  $\mathrm{M}_{30}$  is reduced by increasing  $C_{ST}$  because the effect of  $C_{gd}$  and the change in  $C_{LC}$  becomes small. In the region where  $\text{C}_{\mbox{gd}}/(\text{C}_{\mbox{ST}}\text{+}\text{C}_{\mbox{LCm}})$  is smaller than 0.06 (CST is larger than 0.5pF), M30 begins to saturate because the effect of C<sub>gd</sub> and the change in CLC becomes negligible. The calculated charging time  $(\ensuremath{\text{T}}_r)$  of the TFT is also shown in Fig.8.  $T_r$  is the time required from the time when  ${\tt V}_G$  becomes  ${\tt V}_G({\tt ON})$  to the time when  $V_1$  reaches 90% of source signal voltage.  $T_r$  is increased by increasing  $C_{ST}$ , but it is sufficiently shorter than the gate selecting time of  $63.5\,\mu$  sec. When the storage capacitance of 0.5 pF is added,  $M_{30}$  is lower than 0.055 which is much smaller than without a storage capacitor and Tr is shorter than  $10 \mu$  sec.

Figure 7 also shows  $M_{30}$  as a function of  $\bigtriangleup V_{COM}$  at  $C_{ST}\text{=}0.5 pF. \bigtriangleup V_S$  of 2.8V and 4.5V are the voltages which produce the transmission of 10% and 90%. In comparison with the results without a storage capacitor, the difference of  $\bigtriangleup V_{COM}$  for minimizing  $M_{30}$ , due to  $\bigtriangleup V_S$  change, is nearly eliminated. Further,  $\bigtriangleup V_{COM}$  for minimizing  $M_{30}$  with  $\bigtriangleup V_S$  which produce the transmission of 90% is +1.60V without a storage capacitor, but becomes +0.1V with the storage capacitance of 0.5pF.

### 4.Conclusions

In order to analyze the optical response characteristics of a TFT-LCD, we introduce an equivalent circuit model which takes into account the time dependence and voltage dependence of  $\varepsilon_{\rm LC}$ . The calculated results of the optical response characteristics of the TN-LC cell are in agreement with measurements. We analyzed the 30Hz flicker which appears in the optical rise state of the TFT-LCD due to C<sub>gd</sub> and the change in C<sub>LC</sub>.

The 30Hz flicker is reduced by addition of the storage capacitor.  $M_{30}$  is lower than 0.055, and  $ightarrow V_{COM}$  for minimizing  $M_{30}$  is



Fig.7 M<sub>30</sub> as a function of  $\bigtriangleup V_{COM}$  solid line- $\bigtriangleup V_S$ =3.7V, dashed line- $\bigtriangleup V_S$ =5.0V chain line- $\bigtriangleup V_S$ =2.8V, dotted line- $\bigtriangleup V_S$ =4.5V



Fig.8 M<sub>30</sub> as a function of  $C_{gd}/(C_{ST}+C_{LCm})$  (solid line) and charging time (T<sub>r</sub>) as a function of  $C_{gd}/(C_{ST}+C_{LCm})$  (dashed line)

+0.1V at  $C_{ST}$ =0.5pF. These values are much smaller than without a storage capacitor, and the charging time of the TFT is shorter than 10  $\mu$  sec at  $C_{ST}$ =0.5pF.

#### References

- 1)S.Takahashi, et al.; SID 90 Digest, 11.6, 205(1990)
- 2)T.Onozawa, et al.; Japan Display'89, 15-2, 576(1989)
- 3)Y.Kaneko, et al.; IEEE Trans. Electron Devices, Vol.36,2953(1989)
- 4)T.Yanagisawa, et al.; Japan Display'86, 5.1, 192(1986)
- 5)S.Takahashi, et al.; Japan Display'89, P2-35, 412(1989)
- 6)E.Jakeman and E.P.Raynes; Phys.Lett., Vol.39A, 69(1972)
- 7)S.M.Sze; Physics of Semiconductor Devices, (Wiley, New York, 1981), Chap.8