

Tunnel-Junction-Load SET Logic

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A novel tunnel-junction-load SET logic was proposed and its dynamics was analyzed. It was found that the proposed SET logic has the same simplicity as the resistance-load SET logic and the electron tunneling of the proposed SET logic is suppressed statically as in a complementary SET logic. The tunnel-junction-load SET logic is expected to become standard for future SET integrated circuits.

1. Introduction.

Many new devices using Single Electron Tunneling (SET) have been proposed recently and the dynamic characteristics are being investigated experimentally¹⁻⁴⁾. Logic circuits using SET were proposed^{1,2)} because of its merit of high density and low power consumption. Conventional approaches were:

1) To utilize a load resistor for a pull-up circuit and a Capacitive Single Electron Transistor (CSET) for a pull-down circuit, namely, resistance-load SET logic as shown in Fig.1 (a) proposed by Likharev¹⁾.

2) To utilize two CSETs for both pull-up and pull-down circuits, namely, the complementary SET logic as shown in Fig.1 (b) proposed by Tucker²⁾.

The output voltage in the resistance-load SET logic is unstable because the tunnel current flows statically when the output is low. On the other hand, the circuit of complementary SET logic is more complicated than the resistance-load SET logic just as a CMOS logic is more complicated than an nMOS logic.

In this report, we will propose a novel tunnel-junction-load SET logic to overcome these disadvantages and analyze its dynamics.

2. Tunnel-Junction-Load Logic

Figures 2(a) and (b) show the inverters of a proposed tunnel-junction-load SET logic. Each circuit consists of three tunnel junctions and gate/back-gate capacitances except for an output capacitance. Back-bias voltage V_B controls the input threshold voltage V_{th} . The proposed logic shown in Fig. 2(a) uses the tunnel-junction for a

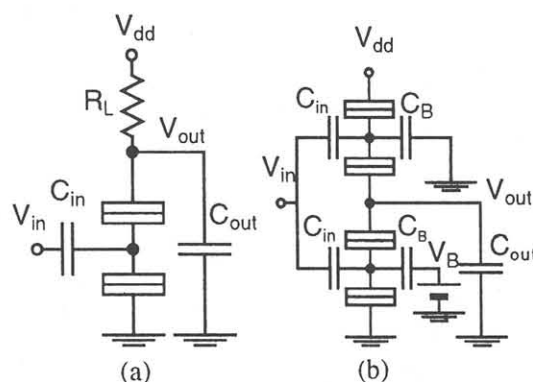


Fig.1. Conventional SET logic circuits: (a) resistance load SET inverter and (b) complementary SET inverter.

pull-up, while conventional SET logics need a CSET or a resistance for a pull-up. On the other hand, the circuit shown in Fig.2(b), which is another way of tunnel-junction-load SET logic, includes a tunnel junction as a pull-down and a CSET as a pull-up, respectively. In both circuits, a simple tunnel junction is used for pull-up or pull-down.

The tunnel-junction-load SET inverter in Fig.2(a) operates as shown in Fig.3. The internal state of the circuit is expressed by the excess charges (q_A, q_B) at nodes A and B, respectively. When the input voltage V_{in} is in the range between 0 and V_{th} , the internal state is (0, 0) and the output is high. As the input voltage increases, the electron firstly tunnels at the junction C_3 and the internal state changes to (0, -e). This state is also stable and the output is low when V_{in} is in the range between V_{th} and V_{dd} . The circuit in Fig.2(b) also operates like

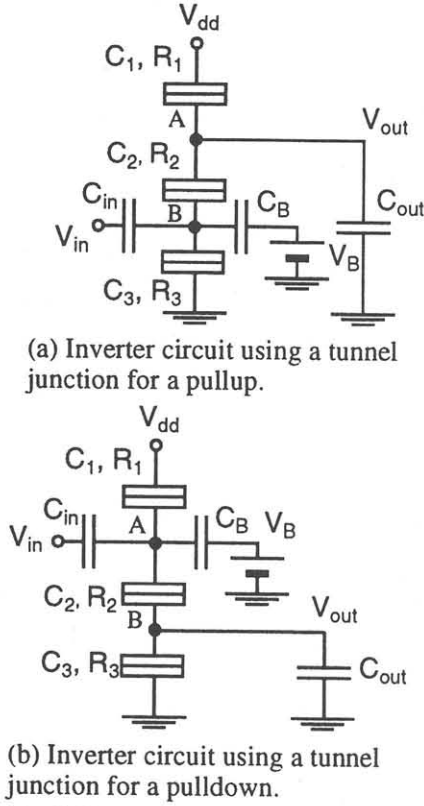


Fig.2. Proposed tunnel-junction-load SET logic. $C_1 = C_2 = C_3 = C_{in}/10 = C_B/10 = C_{out}/10$, $R_1 = R_2 = R_3$.

the circuit in Fig. 2(a).

3. Dynamics of the SET Logic Circuit

When co-tunneling, hot electron effect and quantum fluctuation are negligible, the free energy F of a SET logic is described as follows:

$$F = \frac{1}{2} \mathbf{Q}_i^T \mathbf{M} \mathbf{Q}_i - \mathbf{V}_i^T \mathbf{Q}_i, \text{ and} \quad (1)$$

$$\mathbf{Q}_i = (Q_1, Q_2, Q_3),$$

where Q_i is the charge of electrons tunneling through the junction i , $\mathbf{V}_i$ is the constant vector determined by the source voltage and the prefix t denotes transpose of a matrix or a vector. The first term in Eq. (1) corresponds to the total amount of the electrostatic energy of all capacitances in the logic, and the second term corresponds to the work done by the voltage source. The electron tunneling is suppressed when the free energy of the SET logic increases compared with that before tunneling. Therefore, the condition of Coulomb blockade of the i -th tunnel-junction is given as

$$\left| [M \mathbf{Q}_i - \mathbf{V}_i]_i \right| > \frac{e}{2} m_{ii}, \quad (2)$$

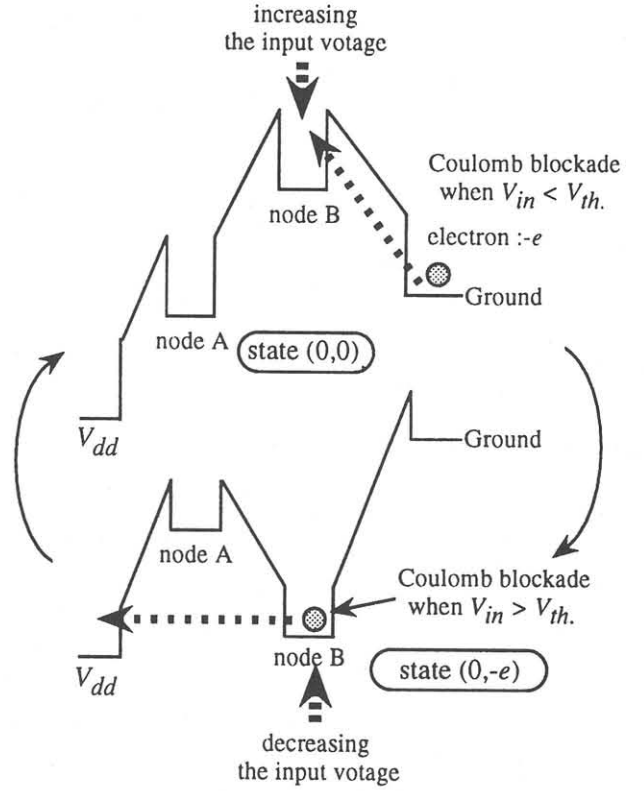


Fig.3. Operating principle of the tunnel-junction-load inverter.

where m_{ii} is the diagonal element of the matrix M and $[]_i$ denotes the i -th element of a vector.

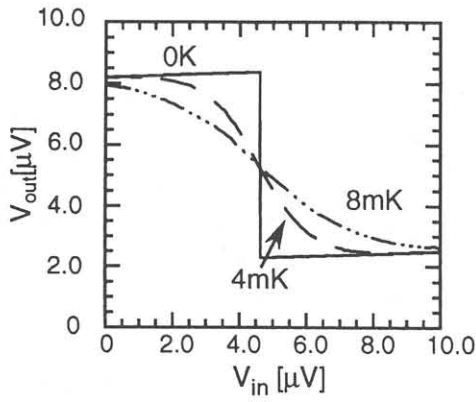
4. Calculation Results and Discussions

Figures 4(a) and (b) show the input-output characteristics obtained by the Monte Carlo simulation, which correspond to two types of circuits shown in Fig.2(a) and (b). They are simulated under the condition of the temperature $T=0K$, $4mK$ and $8mK$, respectively, where $V_{dd}=64\mu V$ and $C=0.1fF$. Although both circuits can operate properly as shown in Figs.4(a) and (b), the voltage gain decreases as the temperature rises in both circuits, which have the same characteristics because of their symmetric structure. V_{th} for Fig. 4(a) is given as

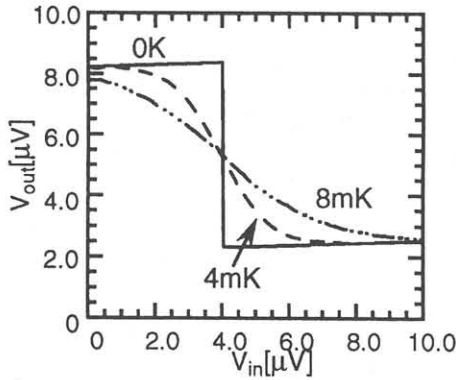
$$V_{th} = \frac{e}{20C} - \frac{V_{dd}}{120} - V_B, \quad (3)$$

which can be derived from Eqs. (1) and (2). By substituting the circuit parameters to Eq. (3), V_{th} is calculated as $4.5\mu V$, which agrees with the results in Fig.4(a).

Figures 5(a) and (b) show the transient waveforms of input and output voltages of the circuit in Fig.2(a). Here, simulation conditions are same as that in Fig. 4(a). It is noted that the electron tunneling is suppressed statically like a complementary CSET logic. Actually electrons tunnel across the tunnel-junctions at a finite tempera-



(a) Characteristic of the circuit shown in Fig.2(a), $V_B=75\mu\text{V}$.



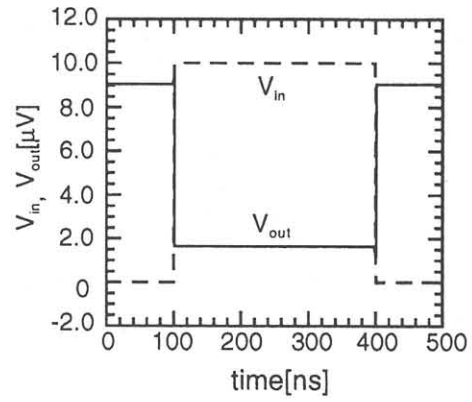
(b) Characteristic of the circuit shown in Fig.2(b), $V_B=210\mu\text{V}$.

Fig.4. Input-output characteristics of the tunnel-junction-load SET inverter. $C_1=C_2=C_3=C_{in}/10=C_B/10=0.1\text{fF}$, $R_1=R_2=R=100\text{k}\Omega$, $V_{dd}=64\mu\text{V}$, $T=8\text{mK}$.

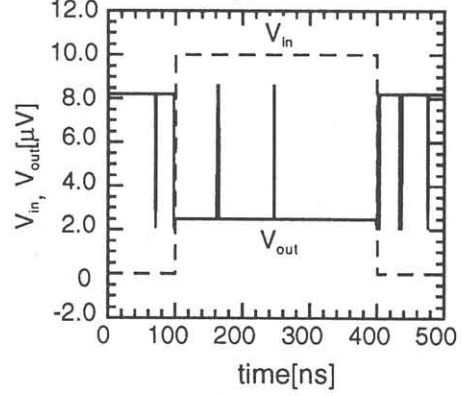
ture, but electrons tunnel across the same junction in opposite direction immediately. This is because the free energy given by Eq.(1) of the circuit becomes minimum at the internal state $(q_A, q_B) = (0,0)$ and $(0,-e)$. In Fig. 6, we calculate the output waveforms of the resistance-load SET logic, the output waveform of which is unstable due to stochastic tunneling events. The output of the tunnel-junction-load SET logic is more stable compared with Fig. 6.

5. Conclusion

We have proposed a novel tunnel-junction-load SET logic and analyzed its dynamics using Monte Carlo method. The proposed SET logic has the same simplicity as the resistance-load SET logic, and has the same stability as complementary SET logic because the electron tunneling of the proposed SET logic is also suppressed statically. The tunnel-junction-load SET logic is expected to become standard for SET integrated circuits in future.



(a) $T=0\text{K}$.



(b) $T=8\text{mK}$.

Fig5. Input and output waveforms of the proposed SET logic. $V_{dd}=64\mu\text{V}$, $V_B=75\mu\text{V}$ and $C=0.1\text{fF}$.

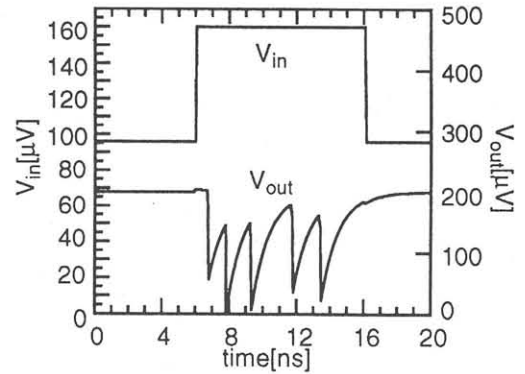


Fig.6. Input and output waveforms of a resistance load SET inverter. $C_1=C_2=C_{in}/5=C_{out}/10=0.1\text{fF}$, $V_{dd}=0.2\mu\text{V}$, $R_1=R_2=R_L/10=100\text{k}\Omega$, $T=92.8\text{mK}$.

References

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