## P2-15

# Influence of Velocity Overshoot on Transport Noise in 0.1-µm MOSFETs

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## **1.Introduction**

MOSFET miniaturization is going beyond the feature size of 100nm (in the laboratory) [1-2]. The conventional approach to MOSFET scaling is based on the empirical scaling rule. However, the signal to noise ratio (dynamic range) degrades as the supply voltage is lowered with down-scaling. In this paper, we theoretically derive carrier-density-fluctuation-induced high-frequency transport noise using a drift-diffusion model and examine noise characteristics in sub-100nm MOSFETs. In addition, we discuss the influence of the velocity overshoot effect (VOE) on transport noise in anticipated short-channel devices.

#### 2. Theorical basis

We consider the carrier-density fluctuation (CDF) in a short-channel nMOSFET being operated in the linear drain current  $(I_D)$  region. It is assumed that dc drain current consists of drift current  $(I_{drift})$  and diffusion current  $(I_{diff})$ , and that it satisfies the current continuity condition. Under this assumption, we derive a partial-differential equation (eq.(1)) for CDF from the charge-density-conservation equation in one dimension;

$$\partial \delta n / \partial t = D_n (\partial^2 \delta n / \partial x^2) - v_d (\partial \delta n / \partial x) - \delta n / \tau^*, \tag{1}$$

$$1/\tau = 1/\tau - (\partial v_d / \partial x). \tag{2}$$

 $D_n$  is the diffusion constant,  $v_d$  is the drift velocity,  $\delta n$  is the CDF,  $\tau$  is the relaxation time for CDF in the quasi-thermal equilibrium condition, and  $\tau$  is the effective relaxation time of fluctuation. Sumino studied the transport noise by using a partial-differential equation that omitted  $I_{diff}$  [3]. In order to consider a more accurate carrier transport phenomena, we analyze the transport noise by using a partial-differential equation (eq.(1)) that includes  $I_{driff}$  and  $I_{diff}$ .

We solve eq. (1) by using Fourier expansion  $(\delta n_m(x))$ based on the conventional Langevin method [4]. Here, we consider the medium-field operation of a MOSFET; that is,  $V_D < E_C L$ , where L is the channel length,  $V_D$  is the drain voltage,  $E_C$  is the critical electric field defined as  $v_s/\mu_{eff}$ ,  $v_s$  is the saturation velocity, and  $\mu_{eff}$  is the effective mobility. Under this condition, CDF  $(\delta n_m(x))$  is given by the superposition of forward  $(\delta n_1(x))$  and backward waves  $(\delta n_2(x))$ ; that is,  $\delta n_m = \delta n_1 + \delta n_2$ . The Wiener-Khintchine theorem [4] gives us the self-correlation function of CDF  $(<\delta n_m \delta n_m^*)$ . In addition,  $<\delta n_m \delta n_m^*$  can be expressed as  $|\delta n_{mo}|^2 T(f, V_D, V_G)$ , where f is the frequency,  $V_G$  is the gate voltage, and  $|\delta n_{mo}|^2$  is the power source of fluctuation; the function  $T(f, V_D, V_G)$  represents modulation of the fluctuation source which is characterized by carrier transport.

The relation between the drain-current noise and CDF

should also be discussed because the drain current noise characteristics, not CDF, are directly observed in MOSFETs. By following the approach of [4], which is based on the quasi-thermal equilibrium approximation, we can obtain an approximation of the spectral density of drain current noise,  $S_{ID}(f)$ , including the transport effect  $(T(f, V_D, V_G))$ .

# 3. Simulation results and discussion

The device parameters used in the simulations are summarized in Table. 1. Figure 1 shows the normalized CDF power (=  $T(f, V_D, V_G)$ ) at f = 1 GHz as a function of the normalized drain voltage  $(V_D/V_{DSAT})$ . Here,  $V_{DSAT}$  is the drain saturation voltage. Figure 1 compares two cases: a very small  $D_n$  value, and a normal  $D_n$  value. The former corresponds to the case in which the contribution of  $I_{diff}$  is effectively neglected [3]. When the  $I_{diff}$  component is taken into account, the fluctuation power is suppressed because the CDF consisting of the forward wave and the backward wave results in wave interference. Figure 2 shows the drain current normalized noise spectral density  $(S_{ID}/(|\delta n_{mo}|^2 I_D^2))$  as a function of  $V_D/V_{DSAT}$ . When the  $I_{diff}$ component is effectively neglected, it can be seen that  $S_{ID}/(|\delta n_{mo}|^2 I_D^2)$  is overestimated in comparison to the case with the normal  $I_{diff}$  component. Thus evaluating  $S_{ID}(f)$ accurately demands that we take into account the  $I_{diff}$ component.

Figure 3 shows  $S_{ID}/(|\delta n_{mo}|^2 I_D^2)$  as a function of  $V_D/V_{DSAT}$ for various L values ranging from 0.1 to 1.0 µm. Here, only L is varied and the other device parameters are fixed at those suitable for a 0.1  $\mu$ m channel device. For all L values,  $S_{ID}/(|\delta n_{mo}|^2 I_D^2)$  is almost independent of  $V_D/V_{DSAT}$  at low V<sub>D</sub> values  $(V_D/V_{DSAT} < 0.1)$  because  $T(f, V_D, V_G)$  is suppressed by the interference of the forward and backward components of CDF (see Fig. 2). For L = 0.5 or  $1.0 \,\mu\text{m}$ ,  $S_{ID}/([\delta n_{mo}]^2 I_D^2)$  is proportional to  $V_D^{0.5}$  at high  $V_D$  values  $(V_D/V_{DSAT} > 0.1)$ . As  $V_D$  increases, the dc channel conductance  $(\partial I_D/\partial V_D)$  decreases, which leads to the saturation of  $I_D$ . Consequently,  $S_{ID}/(|\delta n_{mo}|^2 I_D^2)$  increases with  $V_D$ . For  $L = 0.1 \,\mu\text{m}$ , however,  $S_{ID}/(|\delta n_{mo}|^2 I_D^2)$  is in proportion to  $V_D^{0.3}$  at high  $V_D$  values. When  $V_D$  exceeds a certain value,  $S_{ID}/(|\delta n_{mo}|^2 I_D^2)$  decreases. When L decreases, the effective mobility decreases because of an increase in the longitudinal electric field. Compared to a long channel device, the drain current noise spectral density is relatively suppressed. When  $V_D/V_{DSAT}$  exceeds the certain value, the transport efficiency  $(exp(-L/L_n^*))$  of the CDF power decreases;  $T(f, V_D, V_G)$  decreases, and then  $S_{ID}/(|\delta n_{mo}|^2 I_D^2)$ decreases.  $L_n$  represents the characteristic length of the spatial relaxation of CDF.

Since short-channel MOSFETs, sub-0.1- $\mu$ m channels, should manifest the velocity overshoot effect (VOE) [5], we must discuss the influence of VOE on  $S_{ID}(f)$ . Here, we

consider VOE when calculating  $S_{ID}$  by increasing the low-field mobility ( $\mu_o = 700 \text{ cm}^2/\text{Vs} \rightarrow 900 \text{ cm}^2/\text{Vs}$ ) and the saturation velocity ( $v_s = 1.0 \times 10^7 \text{ cm/s} \rightarrow 3.0 \times 10^7 \text{ cm/s}$ ).  $D_n$  increases with  $\mu_o$  because  $D_n$  is derived from Einstein's relation;  $D_n = 18 \text{ cm}^2/\text{s} \rightarrow 23 \text{ cm}^2/\text{s}$ . Figure 4 shows simulated  $S_{ID}/(|\delta n_{mo}|^2 I_D^2)$  for  $L = 0.1 \text{ } \mu \text{m}$  as a function of  $V_D/V_{DSAT}$ . It can be seen in Fig. 4 that VOE enhances  $S_{ID}/(|\delta n_{mo}|^2 I_D^2)$  at high  $V_D$  values. Since VOE raises the channel conductance and  $L^*_n$ ,  $S_{ID}/(|\delta n_{mo}|^2 I_D^2)$  increases (relatively) when VOE is significant. Consequently, we can suggest that the drain current noise spectral density stemming from CDF is significant in sub-0.1  $\mu \text{m}$  MOSFETs.

## 4.Summary

This paper described theoretical simulation results of carrier-density-fluctuation-induced high-frequency transport noise in short-channel MOSFETs. When the diffusion current component of the drain current is taken into account when calculating the carrier-density fluctuation power, it has been shown that the transferred fluctuation power is reduced. It is predicted that sub-0.1- $\mu$ m channel devices will suffer enhanced drain current noise if the velocity overshoot effect is significant.



Fig.1. The normalized CDF power as a function of  $V_D/V_{DSAT}$ ;  $L = 0.1 \, \mu m$ .



Fig.3.  $S_{ID}/(|\delta n_{mo}|^2 I_D^2)$  as a function of  $V_D/V_{DSAT}$  for various L values ranging from 0.1 to 1.0  $\mu$ m.

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## Table. 1. Device parameters in simulations

Parameters	Values
Channel length (L)	0.1 (µm)
Gate oxide thickness $(t_{ox})$	2 (nm)
Acceptor concentration of substrate $(N_A)$	$10^{18} (\text{cm}^{-3})$
Donor concentration of source and drain $(N_D)$	$10^{20}  (\text{cm}^{-3})$
Low-field mobility $(\mu_o)$	700 (cm <sup>2</sup> /Vs)
Saturation velocity $(v_s)$	$10^{7}$ (cm/s)
Relaxation time for carrier-density fluctuation	
in quasi-thermal equilibrium condition $(\tau)$	$10^{-3}$ (s)



Fig.2.  $S_{ID}/(|\delta n_{mo}|^2 I_D^2)$  as a function of  $V_D/V_{DSAT}$ ;  $L = 0.1 \,\mu\text{m}$ .



Fig.4.  $S_{ID}/(|\delta n_{mo}|^2 I_D^2)$  as a function of  $V_D/V_{DSAT}$ ;  $L = 0.1 \,\mu\text{m}$ . For  $S_{ID}/(|\delta n_{mo}|^2 I_D^2)$  with VOE,  $\mu_0$  and  $v_s$  are increased;  $\mu_0 = 700 \,\text{cm}^2/\text{Vs} \rightarrow 900 \,\text{cm}^2/\text{Vs}$  and  $v_s = 1.0 \times 10^7 \,\text{cm/s} \rightarrow 3.0 \times 10^7 \,\text{cm/s}$ .