

# A New Stable Extraction of Threshold Voltage Using Regularization Method

Woo Young Choi, Byung Yong Choi, Dong-Soo Woo, Myeong Won Lee, Jong Duk Lee, and Byung-Gook Park

Inter-university Semiconductor Research Center and School of Electrical Engineering, Seoul National University

San 56-1, Shinlim-dong, Kwanak-gu, Seoul 151-742, Korea

Phone: +82-2-880-7279 Fax: +82-2-882-4658 E-mail: claritas@korea.com

## 1. Introduction

Threshold voltage ( $V_{TH}$ ) is one of the most important parameters for MOSFET characterization. Many  $V_{TH}$  extraction methods have been proposed to obtain physically-meaningful  $V_{TH}$  from the  $I_{DS}$  versus  $V_{GS}$  characteristics, such as split C-V, linear extrapolation (LE) and transconductance change (TC) method. Among them, only the TC method can yield a result that approaches the classically-defined  $V_{TH}$  [1]. Moreover, it is useful for nanoscale MOSFETs because it eliminates the effects of the interface state, the mobility degradation and the parasitic resistance [2]. Especially in the case of double-gate MOSFETs, the TC method reflects their volume inversion behavior well [3]. However, since in this method the second derivative of  $I_{DS}$  is required, it tends to be very noisy [4]. Numerical differentiation is known to be unstable in that small perturbations of the function to be differentiated may lead to large errors in the computed derivative. In simulation or measurement, most of errors come from round-off and truncation. There is always a trade-off: as nodes are set to be denser, data reflect the rapid variation better while differentiation of the data results in more noise [5]. Fig. 1 shows the importance of node interval selection. If we measure  $g_{m2}$  with 0.05 percent accuracy, noise and detail loss will depend on node interval. When  $\Delta V_{GS}$  is set to be 0.01 V, it is difficult to find  $g_{m2}$  peak due to noise. If we increase  $\Delta V_{GS}$  up to 0.1 V to remove noise, data between nodes will be omitted and then  $g_{m2}$  peak becomes flat. In both cases, we cannot detect the exact  $V_{TH}$ . Thus, we need to optimize the interval to get less noisy  $g_{m2}$  profiles with minimum detail loss. In this paper, we propose a stable extraction method for the  $V_{TH}$  defined by the TC. Adopting it, we can determine  $V_{GS}$  where the surface potential is within  $kT/q$  of  $\phi_s = 2\phi_f + V_{SB}$ . The knowledge of that makes it possible to calculate  $\phi_s$  at any other point on the  $I_{DS}$  versus  $V_{GS}$  curve, which will provide a big help for device analysis.

## 2. Device Design

In the TC method, the  $V_{TH}$  is defined as the  $V_{GS}$  at which the derivative of the low drain voltage transconductance  $dg_m/dV_{GS}$  ( $=g_{m2}$ ) is maximum. Therefore, smooth  $g_{m2}$  profiles without noise lead to the exact  $V_{TH}$ . First, the optimal node interval for  $g_m$  will be derived. When the  $I_{DS}$  is simulated or measured, some errors result from round-off and truncation. We take them into account by introducing an absolute error  $\delta$ . The exact drain current becomes  $I_{DS} = I_{DSm} + \delta$ , where  $I_{DSm}$  is extracted drain current. Considering  $\delta$ , we can get Eq. (1). From (1), Eq. (2) can be derived. The relative error is derived as depicted in Eq. (3). It may look problematic because  $\delta$  is unknown. However, in practice, we can get an error bound for  $\delta$ , that is, a number  $\beta$  such that  $|\delta| \leq \beta$ , where  $\beta$  represents a characteristic sum of errors. Eq. (3) becomes Eq. (4). If we want less than one-percent error in  $g_m$ , the condition is derived as shown in Eq. (5). For  $g_m$  is approximated to  $\Delta I_{DS} / \Delta V_{GS}$ , the optimal interval for  $g_m$  is defined as in Eq. (6). Referring to results above, the optimal node interval for  $g_{m2}$  is obtained. Assuming  $g_m = g_{mm} + \varepsilon$ , the case is the same.  $g_m$  is the true value of  $dI_{DS} / dV_{GS}$ ,  $g_{mm}$  is the  $dI_{DS} / dV_{GS}$  from Eq. (1) to (6) and  $\varepsilon$  is the calculation error. Note that  $g_{mm}$  means  $g_m$  in Eq. (1) to (6). We obtained the optimal node interval for  $g_{m2}$  as shown in Eq. (7) where  $\gamma$  means an error bound for  $\varepsilon$ , which requires  $|\delta| \leq \gamma$ . From the condition of one-percent error above, it is found that  $\gamma$  is equal to 0.01 times  $g_m$ . Thus, Eq. (7) can be rewritten into Eq. (8). To profile  $g_{m2}$  with minimum loss of details, conditions (6) and (8) should be satisfied at

the same time. Finally, the optimal node interval for accurate  $g_{m2}$  becomes Eq. (9). By this criterion, noise-free  $g_{m2}$  is obtained within one percent error.

The condition (9) is applied to the simulation by estimating next node interval from  $g_m$  and  $g_{m2}$  derived referring to previous three data nodes. Fig. 2 shows the flow chart for optimal node extraction. When initial values of  $I_{DS}$ ,  $g_m$  and  $g_{m2}$  are given, the optimal interval for next  $V_{GS}$  is calculated according to Eq. (9). After obtaining the drain current value of the given  $V_{GS}$ , we perform the second order differentiation to extract noise-free  $g_{m2}$  without detail loss. Then, the values of  $I_{DS}$ ,  $g_m$  and  $g_{m2}$  are fed back into the first stage. The algorithm leads to  $g_{m2}$  profiles satisfying one-percent noise criterion as shown in Fig. 3. The simulation was done to a 1.5  $\mu\text{m}$  nMOSFET at 0.1 V drain bias. Considering the noisy profiles in Fig. 1, the improvement is prominent.  $V_{TH}(P)$ ,  $V_{TH}(LE)$  and  $V_{TH}(TC)$  represent the  $V_{TH}$  of the classical definition ( $\phi_s = 2\phi_f + V_{SB}$ ), the LE and the TC method, respectively.  $V_{TH}(LE)$  is selected because it is *defacto* industry standard.  $V_{TH}(TC)$  extracted by our algorithm approaches  $V_{TH}(P)$ . To generalize our algorithm, we compared three  $V_{TH}$ 's in various channel lengths. In long channel,  $V_{TH}(TC)$  predicts  $V_{TH}(P)$  within  $kT/q$  as shown in Fig. 4. The same is the case in short channel, as depicted in Fig. 5. Moreover,  $V_{TH}(TC)$  reflects more precise  $V_{TH}$  roll-off than  $V_{TH}(LE)$ . To make this behavior clear, correlation coefficients are calculated. The correlation coefficient  $R_{xy}$  for  $x$  and  $y$  is defined in Eq. (10). Table 2 shows better correlation between  $V_{TH}(P)$  and  $V_{TH}(TC)$ . We also performed the fast Fourier transform to confirm that our algorithm extracts noiseless  $g_{m2}$  profiles without detail loss. Fig. 6 proves that it eliminates noise components without loss of  $g_{m2}$ . Noise in high frequency range are suppressed as intervals are optimized, while data in low frequency range remain the same. If intervals exceed optimum, the peak in low frequency will be lowered due to data loss.

## 3. Conclusions

Consequently, it is found that our algorithm extracts noiseless  $g_{m2}$  profiles without detail loss and that  $V_{TH}(TC)$  derived from the  $g_{m2}$  profiles predicts  $V_{TH}(P)$  within  $kT/q$ . This  $V_{TH}$  extraction reflects the  $V_{TH}$  roll-off of nanoscale MOSFETs accurately and makes it possible to calculate the  $\phi_s$  at any other point on the  $I_{DS}$  versus  $V_{GS}$  curve. Finally, the algorithm will endow us with powerful methodology in device modeling and characterization.

## Acknowledgements

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## References

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Table 1. Equations for optimal node interval derivation.

$g_m + dg_m = dI_{DSm} / dV_{GS} = d(I_{DS} - \delta) / dV_{GS}$ $= dI_{DS} / dV_{GS} - d\delta / dV_{GS}$	(1)
$dg_m = -d\delta / dV_{GS}$	(2)
$dg_m / g_m = - (d\delta / dV_{GS}) / (dI_{DS} / dV_{GS})$ $= -d\delta / dI_{DS} \approx \Delta \delta / \Delta I_{DS}$	(3)
$dg_m / g_m \approx \Delta \delta / \Delta I_{DS} = 2\beta / \Delta I_{DS}$	(4)
$\Delta I_{DS} \geq 200\beta$	(5)
$\Delta V_{GS} = \Delta I_{DS} / g_m \geq 200\beta / g_m$	(6)
$\Delta V_{GS} = \Delta g_m / g_{m2} \geq 200\gamma / g_{m2}$	(7)
$\Delta V_{GS} \geq 2g_m / g_{m2}$	(8)
$\Delta V_{GS} \geq \max(200\beta / g_m, 2g_m / g_{m2})$	(9)
$R_{xy} = \text{cov}(x,y) / \sigma_x \sigma_y$	(10)

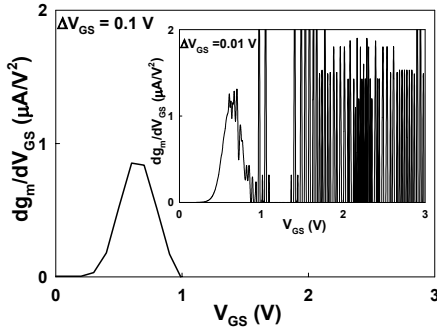


Fig. 1. Comparison of  $g_{m2}$  when node interval is 0.1 V. Inset figure shows 0.01 V case.

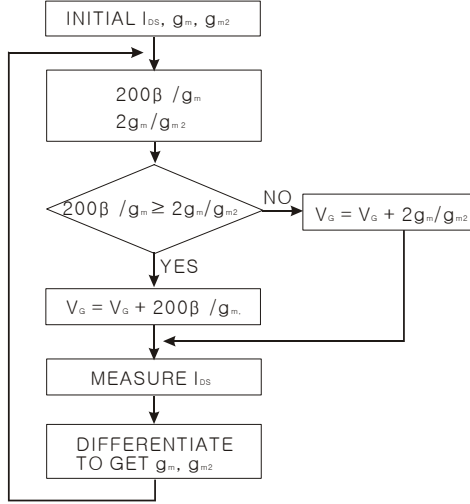


Fig. 2. Algorithm for optimized node interval derivation. Referring to previous three data points,  $\Delta V_{GS}$  is determined.

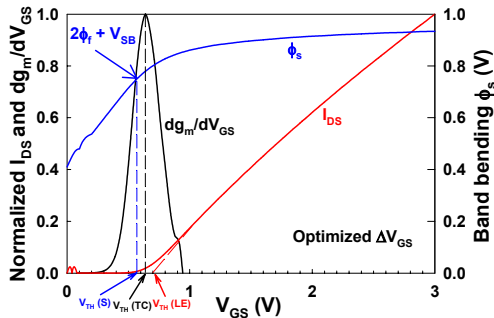


Fig. 3. Optimized  $g_{m2}$  profiles calculated from the algorithm for optimized node interval. (1.5  $\mu\text{m}$  nMOSFET)

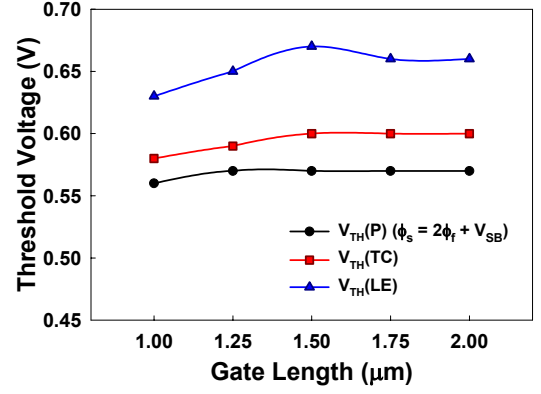


Fig. 4. Comparison of threshold voltage in long channel MOSFETs.  $V_{TH}(TC)$  shows better correlation to  $V_{TH}(P)$  than  $V_{TH}(LE)$ .

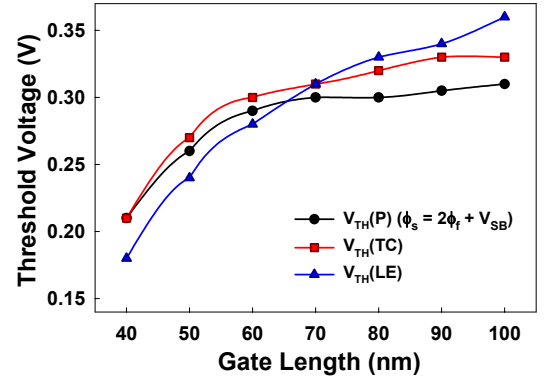


Fig. 5. Comparison of each threshold voltage in short channel MOSFETs.  $V_{TH}(TC)$  shows better correlation to  $V_{TH}(P)$  than  $V_{TH}(LE)$ . In addition,  $V_{TH}(TC)$  reflects more precise threshold voltage roll-off characteristics than  $V_{TH}(LE)$ .

Table 2. Correlation coefficients calculated from the pairs of the threshold voltages in Fig. 4 and Fig. 5.

	Correlation coefficient between $V_{TH}(P)$ and $V_{TH}(TC)$	Correlation coefficient between $V_{TH}(P)$ and $V_{TH}(LE)$
Long channel MOSFETs	0.953	0.884
Short channel MOSFETs	0.994	0.945

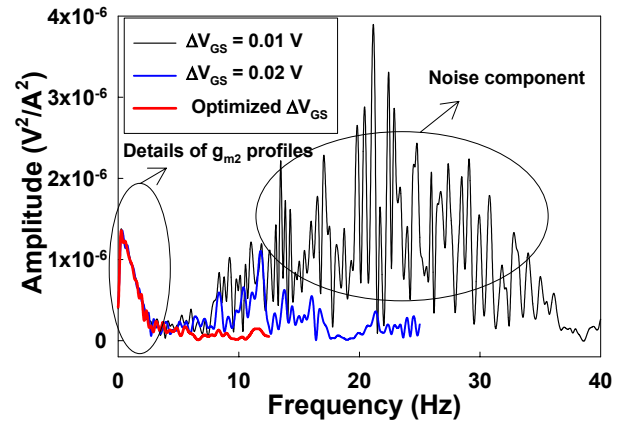


Fig. 6. Fast Fourier transform of  $g_{m2}$  profiles with variation of node intervals. Noise components in high frequency range are suppressed as node intervals get optimized, while detailed data in low frequency range remain the same.