# Measurement of electron spin states in a semiconductor quantum well using tomographic Kerr rotation 

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Fig. 1 The rotations of probe light beam polarization
pulse polarization [3].
The rotation of the probe light beam polarization tells us the electron spin state by appropriately selected measurement. Table 1 summarizes the combination of input polarization of the probe light beam, measurement basis of the Kerr rotation, and projection basis of the electron spin state. For instance, we have already reported the $y$-axis projection of the electron spin state measured by the circularly polarized $\sigma^{ \pm}$probe light beam, which consists of a linear superposition of two linear polarizations $\mathrm{D}^{ \pm}$. With the coherent transfer scheme, the $\mathrm{D}^{ \pm}$polarized light beam virtually creates the electron spin states $| \pm y\rangle_{\mathrm{e}}=\left(|\uparrow\rangle_{\mathrm{e}}\right.$ $\left.\pm i|\downarrow\rangle_{\mathrm{e}}\right) / \sqrt{ } 2$, and the Kerr rotation arises from the exchange interaction $\mathbf{s}_{1} \cdot \mathbf{s}_{2}$.

Here, we demonstrate the $y$-axis projection of the electron spin state with the conventionally used linear polarized beam light beams ( H and V ). As seen in Table 1, the $y$-axis projection of the electron spin state is indicated by measurement of the Kerr rotation on the circularly polarized $\sigma^{ \pm}$basis. It is necessary, however, to keep in mind the magnetic circular dichroism (MCD) effect [4], which is induced by the difference between the optical absorption efficiency of the two circular polarizations $\sigma^{ \pm}$, and causes rotation of the probe light beam polarization as shown in Fig. 1. The MCD effect must be removed from the rotations to measure the $y$-axis projection with the tomographic Kerr rotation method.

## 3. Experimental setup and result

In this demonstration, we used a GaAs/AlGaAs quantum well in which g-factors are controlled so we could apply the coherent transfer scheme. The electron and light-hole (LH) g-factor under an in-plane magnetic field in this quantum well are -0.2 and -3.5 , respectively. Therefore, a magnetic field $B_{x}=7 \mathrm{~T}$ causes the Zeeman splitting of the light hole, and reconfigures it into the superposed eigenstates $| \pm \mathrm{x}\rangle_{\mathrm{LH}}=\left(|\uparrow\rangle_{\mathrm{LH}} \pm \mathrm{i}|\downarrow\rangle_{\mathrm{LH}}\right) / \sqrt{2}$. When one of two light-hole states is virtually excited by the probe light, the tomographic Kerr rotation method is applicable. The pump and probe light beam are generated by spectrally filtering the same light beam from a mode-locked Ti:sapphire laser delivering 130 -fs pulses at a reputation rate of 76 MHz , and a variable delay line was set in the probe path. The pump wavelength for the experiments is set to 796.7 nm , which corresponds to $|-\mathrm{x}\rangle_{\mathrm{LH}}$, and the probe wavelength is set to 795.0 nm , which corresponds to $|+\mathrm{x}\rangle_{\text {LH }}$. We selected the different LH states for the pump and probe light beam to avoid their interference effect.

We prepare the electron spin state $|\uparrow\rangle_{\mathrm{e}}+\mathrm{i}|\downarrow\rangle_{\mathrm{e}}(+\mathrm{y})$ that precess about the static magnetic field $B_{x}$ by the pump light beam, and project these electron spins on two mutu-ally-orthogonal bases (z-axis and y-axis) in the Bloch sphere. The $y$-axis projection is measured by the Kerr rotation on the circularly polarized $\sigma^{ \pm}$basis. Therefore, we construct an apparatus to measure the rotation of the polarization on the $\sigma^{ \pm}$basis, as shown in Fig. 2. Using the quarter wave plate, the rotation on the $\sigma^{ \pm}$basis is converted to the $\mathrm{H}-\mathrm{V}$ basis, which is spitted by the polarization beam splitter. This apparatus also allows measurement of the $\mathrm{D}^{ \pm}$basis by replacing the quarter wave plate with the half wave plate. Fig. 3 shows the result of the tomographic Kerr rotation measurement of the precessing electron spins at 10 K . The result shows us that the $y$-axis projection is delayed by $\pi / 2$ from the $z$-axis projection. We can recognize from this result that the projection bases are orthogonal

To remove the MCD effect, we use two types of probe light beam polarization ( H and V ). In this measurement, the Kerr rotation indicates the positive and negative signals with the H probe and V probe, respectively. In contrast, the MCD effect indicates the same signed signal with each of the probe polarizations. Applying this difference between


Fig. 2 Experimental setup for the $y$-axis projection. (QWP, quarter wave plate; PBS, polarization beam splitter; PD, photo detector). To split by the polarization beam splitter, the rotation on the $\sigma^{ \pm}$basis must be converted to the $\mathrm{H}-\mathrm{V}$ basis.


Fig. 3 The tomographic Kerr rotation measurement of the precessing electron spins with an in-plane magnetic field $\mathrm{Bx}=7 \mathrm{~T}$. Each of projections is measured by two linear polarized probe light beams ( H and V ).
the Kerr rotation and the MCD effect, we subtract these two signals of eq. (1) and eq. (2). Accordingly, we can permit the distinction between the Kerr rotation and the MCD effect.

$$
\begin{align*}
& \text { Signal }(H)=\text { Signal }(\text { Kerr })+\text { Signal }(M C D)  \tag{1}\\
& \text { Signal }(V)=- \text { Signal }(\text { Kerr })+\text { Signal }(M C D) \tag{2}
\end{align*}
$$

Our pervious measurement of the $y$-axis projection used the circularly polarized probe light beam $\sigma^{ \pm}$. Inconveniently, it was necessary to change the polarization of the probe light beam for the z -axis projection. In contrast, the new scheme provides a technique for the measurement of both the $y$-axis and $z$-axis projection by the same probe light beam polarization.

## 4. Conclusions

We were able to measure the $y$-axis projection of the electron spins with the linear polarizations (H and V). This result shows that the tomographic Kerr rotation method, except in the case of the x -axis projection, is applicable by the same probe light beam polarization. In addition, we demonstrate an effective method for distinguishing between the Kerr rotation and the MCD effect. As a consequence, the tomographic Kerr rotation method allows measurement of the $y$-axis and $z$-axis projection of the electron spin state by merely selecting the measurement basis of the Kerr rotation.

## Acknowledgements

This work was supported by CREST-JST, ERATO-JST, SCOPE-MIC, MEXT, and NEDO.

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