# Development of Multi-Scale Simulation Method for Dye-Sensitized Solar Cells Including Effect of Photoelectrode Material Interface

Mari Onodera<sup>1</sup>, Ryo Nagumo<sup>2</sup>, Ryuji Miura<sup>1</sup>, Ai Suzuki<sup>2</sup>, Hideyuki Tsuboi<sup>3</sup>, Nozomu Hatakeyama<sup>3</sup>, Akira Endou<sup>3</sup>, Hiromitsu Takaba<sup>1</sup>, Momoji Kubo<sup>4</sup>, and Akira Miyamoto<sup>2,1,3</sup>

<sup>1</sup>Tohoku Univ., Dept. Chem. Eng., Grad. School Eng., 6-6-10-205 Aoba, Aramaki, Aoba-ku, Sendai 980-8579, Japan Phone: +81-22-795-7237 E-mail: mari@aki.che.tohoku.ac.jp

<sup>2</sup>Tohoku Univ., NICHe, 6-6-10-205 Aoba, Aramaki, Aoba-ku, Sendai 980-8579, Japan

<sup>3</sup>Tohoku Univ., Dept. Appl. Chem., Grad. School Eng., 6-6-10-205 Aoba, Aramaki, Aoba-ku, Sendai 980-8579, Japan <sup>4</sup>Tohoku Univ., FRI, Grad. School Eng., 6-6-11-701 Aoba, Aramaki, Aoba-ku, Sendai 980-8579, Japan

## 1. Introduction

Dye-Sensitized Solar Cells (DSSCs) are regarded as next-generation solar cells since O'Regan and Grätzel's report [1]. Features of DSSC are low-cost production, wide variety of designs, independence of installation sites, etc. The maximum conversion efficiency of DSSC is about 11% [1]. Further improvement highly relies on better understanding of the energy conversion mechanisms and precise modeling for design optimization [2].

Recent studies showed that under an open-circuit condition, current flow through the interface between  $TiO_2$  and the transparent conducting oxide (TCO) at the photoelectrode occurred due to the recombination of electrons with oxidized redox mediators  $(I_3^-)$  at the TCO/electrode interface [3,4]. Therefore, the effect of the TiO<sub>2</sub>/TCO interface on the current density (*J*) - voltage (*V*) characteristics has been regarded to be significant. The voltage loss at the TiO<sub>2</sub>/TCO interface can be modeling by Schottky barrier model based on the thermionic-emission theory [2].

We have developed a multi-scale DSSC simulator [5,6]. This method includes the effects of the irregular  $TiO_2$  porous structure and the electrolyte. However, the internal resistances in construction materials have not been considered.

In this study, we developed the calculation part for the voltage loss at the TiO<sub>2</sub>/TCO interface and implemented it to our DSSC simulator. The effect of Schottky barrier height derived from the TCO material on the J-V characteristics was evaluated employing the cis-di(thiocyanato)-bis(2,2'-bipyridyl-4,4'-dicarboxylicacid) -ruthenium(II) (N3 dye) as a photosensitizer [7].

### 2. Methods

*Micro-scale simulation: Estimation of oscillator strength of dye* 

We calculated the oscillator strength of N3 dye using our tight-binding quantum chemical calculation program, "Colors" [8].

Meso-scale simulation(1): Construction of  $TiO_2$  porous structure model

We constructed the irregular  $TiO_2$  porous structure model using the three-dimensional porous structure

simulator, "POCO<sup>2</sup>" [9] (Fig. 1).

*Meso-scale simulation(2): Electron Diffusion Simulation* 

The electron diffusion coefficient in constructed  $TiO_2$  porous model was estimated by performing the electron diffusion simulation [5]. The injected electrons from dyes flow in the  $TiO_2$  network toward TCO following the trapping-detrapping process.

Meso-scale simulation(3): Tortuosity Simulation

After donating electrons to the conduction band of  $TiO_2$ , the oxidized dye is reduced by  $\Gamma$  in the electrolyte. To take into account the effect of the electrolyte between  $TiO_2$ particles, we calculated the tortuosity of the  $TiO_2$  porous model by the tortuosity simulator [6].

### Macro-scale simulation: J-V Characteristics simulation

Using the results of micro- and meso-scale simulations, J-V characteristics of DSSC devices was estimated. In this study, we developed the calculation part for the voltage loss at the TiO<sub>2</sub>/TCO interface and implemented it in J-V characteristics simulator. Fig. 2 shows the previous [6] and



Fig. 2 Simulation flow for J-V characteristics. Solid line shows the new method including the effect of TiO<sub>2</sub>/TCO interface. Dotted line shows the previous method.

new simulation flow. The voltage loss at the  $TiO_2/TCO$  interface  $V_1$  is expressed as Eq. (1) [2],

$$V_{1} = \frac{kT}{e} \ln \left[ 1 + \frac{J}{A^{*}T^{2} \exp(-e\phi_{b}/kT)} \right]$$
(1)

where k is the Boltzmann constant; T is the absolute temperature; e is the elementary electric charge; J is the current density;  $A^*$  is the Richardson constant of TiO<sub>2</sub>;  $\Phi_b$  is the Schottky barrier height.

#### 3. Results and Discussion

We calculated the oscillator strength of N3 dye. This result is same to the previous study and the details have been reported in our previous paper [6].

Meso-scale simulations were performed to the constructed model (Fig. 1). Results and parameters are shown in Table 1.

Using the obtained micro- and meso-results, we simulated *J-V* characteristics. We used the value of  $1.3 \times 10^{-10}$  mol cm<sup>-2</sup> for the concentration of N3 dye, which was calculated for the monolayer adsorption on an ideal flat surface of TiO<sub>2</sub> [10]. The intensity of incident light  $\Phi(\lambda)$  of the AM 1.5 solar spectrum [11] is used for the calculation.

Fig. 3 shows the *J-V* curve comparison between the previous method [6] and the new method including  $V_I$ . New method is in better agreement with an experimental result [7] than the previous one. Fig. 4 shows the simulated *J-V* curve with different  $\Phi_b$ .  $V_{OC}$  increases with decreasing  $\Phi_b$ . Moreover, the effect of  $\Phi_b$  tends to be significant as  $\Phi_b$  increases. When  $\Phi_b$  is 0.5, 0.6, and 0.7 eV, the TCO material is assumed to be Al, FTO, and Au, respectively [12]. In the cases of *J-V* curves corresponding to FTO and Au, simulated *J-V* characteristics are qualitatively consistent with Kron's experimental data [12].

#### 4. Conclusions

In this study, we newly developed a DSSC simulator for J-V characteristics including the effect of the TiO<sub>2</sub>/TCO interface. Our simulator successfully predicted the effect of  $\Phi_b$  on  $V_{OC}$  as well as J-V characteristics. By this improvement, the relationship between the TCO material and the performance of DSSC devices can be shown.

Table 1 Meso-scale simulation results and parameters.

Parameter	Value
Porosity / -	0.5
Overlap ratio / -	0.5
Average radius / nm	20
Number of electrons / -	12,500
Electron diffusion coefficient / $cm^2 s^{-1}$	$1.24 \times 10^{-4}$
Tortuosity / -	1.66

![](_page_1_Figure_12.jpeg)

Fig. 3 The comparison between the new J-V simulation method including the TiO<sub>2</sub>/TCO voltage loss and the previous method.

![](_page_1_Figure_14.jpeg)

Fig. 4 The effect of  $TiO_2/TCO$  Schottky barrier hight on *J-V* characteristics.

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