

# Strain Effect on Electronic Properties Tuning of Bilayer WS<sub>2</sub>

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## Abstract

**Strain effect on the electronic properties of bilayer WS<sub>2</sub> is investigated by density functional theory (DFT). With biaxial strain, the band gap and carrier effective masses of AA and AB stacking bilayer WS<sub>2</sub> reduce with tensile biaxial strain. But their band gap increase first under small compressive strain and then decrease with larger compressive strain. This phenomenon can be understood by the detail of the electronic wave-function distribution and interplay of S<sub>p</sub>- and W<sub>d</sub>-orbitals. The electronic properties of AA and AB stacking bilayer WS<sub>2</sub> with uniaxial strain are also studied.**

## 1. Introduction

Recently transition metal dichalcogenides have attracted tremendous attentions. Among them, two-dimensional single/multi-layer MoS<sub>2</sub> were first fabricated and enormously investigated. However, several investigations suggested that WS<sub>2</sub> outperforms MoS<sub>2</sub> as the transistor channel material [1]. Hence, researches on WS<sub>2</sub> are in highly demand. In this paper, both biaxial and uniaxial strain is applied to AA and AB stacking bilayer WS<sub>2</sub> to the tuning of electronic properties. The first principles approach is used to investigate the strain effect. Electronic wave-function distribution and interplay of S<sub>p</sub>- and W<sub>d</sub>-orbitals as well as carrier effective masses are analyzed. Based on the results, an integrated parameter is defined to explain the strain effect.

## 2. Calculation Method and Strain Model

Density Functional Theory approach (DFT) with ultra-soft pseudo-potential (USPP) implemented in CASTEP package was employed to perform the calculation. Exchange and correlation energy was approximated by generalized gradient approximation (GGA) with PW91. The energy cutoff for charge density was set to 600 eV. The van de walls interaction was also considered. Geometric optimization was completed until the maximum force was less than 0.02 eV/Å. The band gap of bulk WS<sub>2</sub> with lattice constant of  $a=3.153\text{\AA}$  after relaxation was 0.97eV, which agrees well with previous work [2]. The AA and AB stacking bilayer WS<sub>2</sub> was constructed from bulk WS<sub>2</sub> (shown in Fig.1 (b) and (c)). Biaxial strain was applied to bilayer WS<sub>2</sub> with rhombus super-cell structure via changing the lattice constants as shown in Fig.1 (a). The rectangle super-cell of WS<sub>2</sub> was shown in Fig. 1 (d). The uniaxial strain was applied to bilayer WS<sub>2</sub> along x+y and x-y direction. The electronic properties affected by symmetrical biaxial strains were performed along irreducible path GMKG while asymmetrical uniaxial strains were calculated along GMKNLG shown in Fig.1 (e).

## 3. Results and Discussion

As shown in Fig. 2 and 4, AA stacking bilayer WS<sub>2</sub> has relatively larger band gap than AB stacking bilayer WS<sub>2</sub> due to different atoms arrangement. It can be seen from Fig.2 (b) the arrangement of AA stacking results in less electron overlap between two layers, which leads to larger band gap. For bilayer WS<sub>2</sub>, the compressive biaxial strain makes Q valley lower than K point while the tensile strain lowers K valley [3]. This can be understood by the quantum quantization effect along layer thickness direction and consistent with the indirect-direct transition of monolayer MoS<sub>2</sub> [4]. The carrier effective masses reduce as tensile biaxial strain increases. However, under compressive strain, electron effective masses decrease but the tendency of hole effective masses is a little complex, related to

the position of valence band maximum (VBM).

From Table.1, the thickness of bilayer WS<sub>2</sub> can be enlarged by compressive biaxial strain and then p-orbits of S atoms (S<sub>p</sub>-orbitals) contribute more than d-orbitals of W atoms (W<sub>d</sub>-orbitals) to conduction band minimum (CBM) and VBM. On the contrary, tensile biaxial strain decreases the thickness of bilayer WS<sub>2</sub> and W<sub>d</sub>-orbitals contribute more. This can be seen in Fig. 3 in which the electronic wave-function distribution at CBM and VBM of AB stacking bilayer WS<sub>2</sub> with  $\varepsilon=-9.6\%$  and  $\varepsilon=10\%$  respectively are plotted. The band gap of bilayer WS<sub>2</sub> decreases with increasing tensile biaxial strain. When compressive strain is applied, the band gap increases first and then decreases to 1.1eV and 1 eV, respectively for AA and AB stacking as shown in Fig.4. This can be understood by the interplay between S<sub>p</sub>- and W<sub>d</sub>-orbitals. We define an integrated parameter N as follows, which can describe the S<sub>p</sub>- and W<sub>d</sub>-orbitals interplay

$$N = \frac{\int f(E_d)dE}{\int f(E_p)dE} \quad (1)$$

where  $f(E_d)dE$  is the W<sub>d</sub>-orbitals contribution to electron wave function. N<sub>CBM</sub> means this parameter is calculated near CBM.

The parameter N with various strains is plotted in Fig. 5. The larger the parameter, the more W<sub>d</sub>-orbitals like the electron state is. And larger integrated parameter N means lower CBM and VBM [5]. Thus if N<sub>CBM</sub> decreases slower or increases faster than N<sub>VBM</sub>, the band gap will decrease, but if N<sub>CBM</sub> decreases faster than N<sub>VBM</sub> the band gap will increase. It can be seen that the decreasing faster N<sub>CBM</sub> than N<sub>VBM</sub> in smaller compressive strain regime can explain the abnormal band gap increase in Fig. 4.

The influence of uniaxial strain to AA and AB stacking bilayer WS<sub>2</sub> is also investigated. The band structure and PDOS of strained AB stacking bilayer WS<sub>2</sub> are plotted in Fig.6. The uniaxial strain had similar modulation effect to bilayer WS<sub>2</sub> with biaxial strain. And it can be observed that the tuning effect of uniaxial strain is weaker than that of biaxial strain. With 10% tensile uniaxial strain, AB stacking bilayer WS<sub>2</sub> has band gap of 0.69 eV and 0.79 eV respectively for the uniaxial strain in x+y direction and x-y direction. The parameter N and carrier effective masses affected by uniaxial strain also have the alike tendency with those influenced by biaxial strain.

## 3. Conclusions

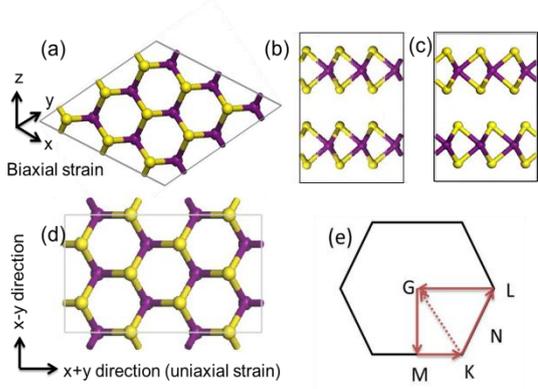
The electronic properties of both AA and AB stacking bilayer WS<sub>2</sub> affected by biaxial and uniaxial strain are studied. Tensile strain will reduce the band gap and carrier effective masses while small compressive strain will increase and large compressive strain will decrease the band gap. Analysis on electronic wave-function distribution and interplay of S<sub>p</sub>- and W<sub>d</sub>-orbitals can be used to explain above results. This work can be a useful reference to broaden the application of strain engineering technology to WS<sub>2</sub> based electrical devices.

## Acknowledgements

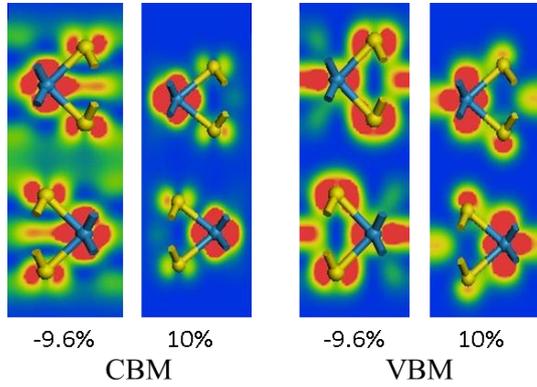
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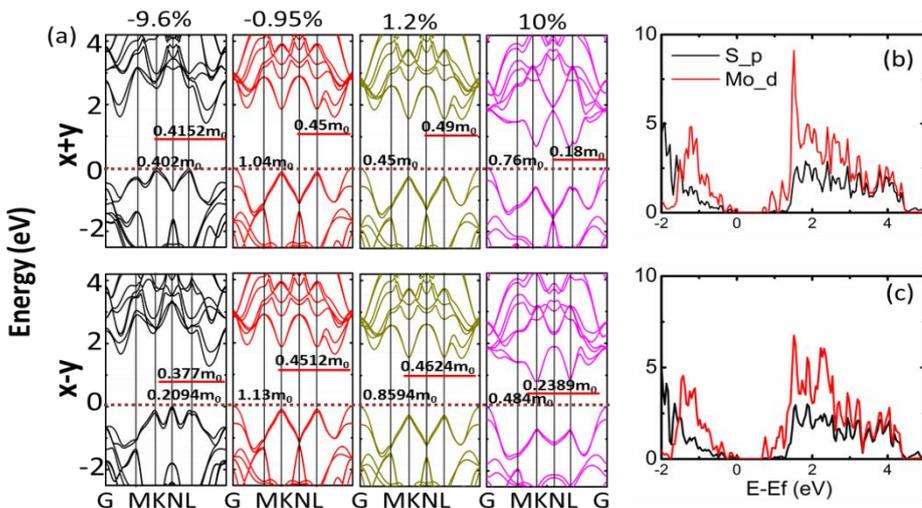
**Fig.1** (a). Top view of WS<sub>2</sub> with rhombus super-cell. Biaxial strain is applied to bilayer WS<sub>2</sub> along both x and y direction. (b). AA stacking bilayer WS<sub>2</sub>. (c). AB stacking bilayer WS<sub>2</sub>. (d). Top view of WS<sub>2</sub> with rectangle super-cell. The uniaxial strain is applied respectively along x+y direction and x-y direction. (e). Irreducible Brillouin zone of WS<sub>2</sub>. Biaxial strains were performed along path GMKG while uniaxial strains were calculated along path GMKNLG. Red and yellow balls indicate W and S atoms.



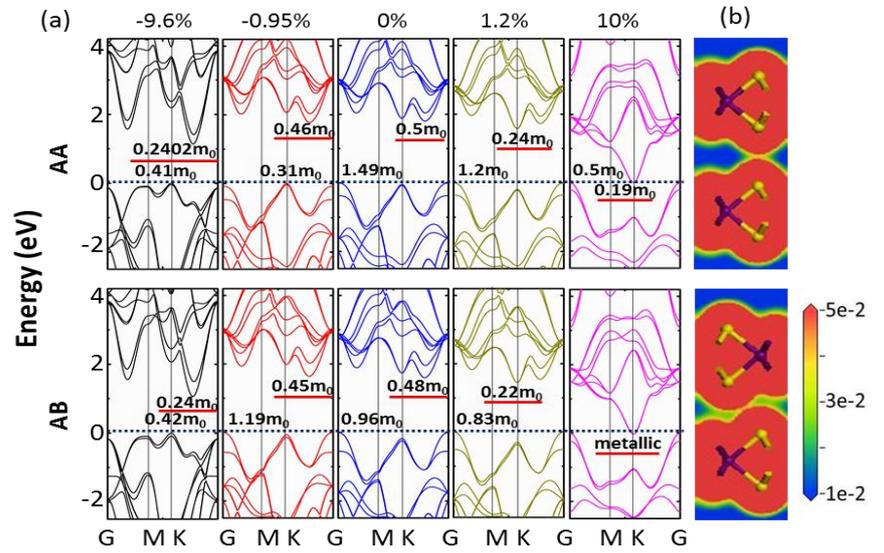
**Fig.3** Wave function distribution of biaxial strained AB stacking bilayer WS<sub>2</sub> with  $\varepsilon=-9.6\%$  and  $10\%$  at CBM and VBM.

**Table.1** distances between atoms in sandwich structure for biaxial strained bilayer WS<sub>2</sub> with various strains strength

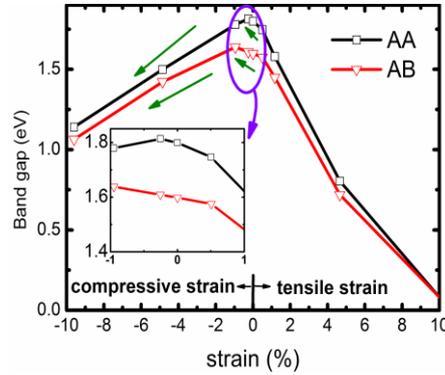
Strain	-9.6%		-0.95%		0%		1.2%		10%	
Distance	$d_{w-s}$ (Å)	$d_{s-s}$ (Å)								
AA stacking	2.367	3.401	2.404	3.180	2.410	3.158	2.417	3.132	2.492	2.965
AB stacking	2.366	3.400	2.404	3.179	2.408	3.163	2.417	3.132	2.491	2.963



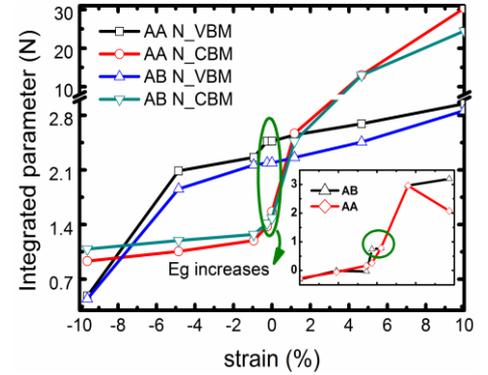
**Fig.6** (a). Band structures along irreducible path of GMKNLG and carrier effective masses of AB stacking bilayer WS<sub>2</sub> with x+y and x-y direction uniaxial strain,  $\varepsilon=-9.6\%$ ,  $-0.95\%$ ,  $1.2\%$  and  $10\%$  (b) and (c). PDOS of AB stacking bilayer WS<sub>2</sub> with uniaxial strain,  $\varepsilon=10\%$  in x+y and x-y direction, respectively.



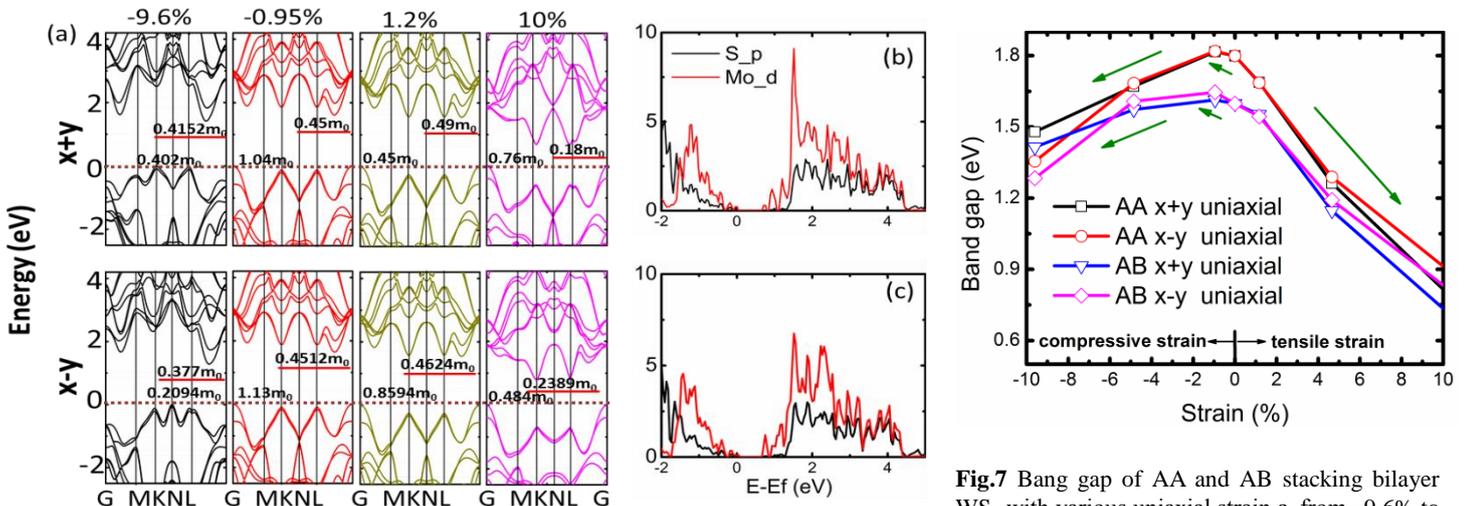
**Fig.2** (a). Band structure of AA stacking and AB stacking bilayer WS<sub>2</sub> with biaxial strain,  $\varepsilon=-9.6\%$  to  $10\%$ . And the carrier effective masses are also labeled. (b) and (c). Electron density of unstrained AA and AB stacking bilayer WS<sub>2</sub>. The upper one is of AA stacking bilayer WS<sub>2</sub> and the lower one is of AB stacking one.



**Fig.4** Band gap of AA stacking and AB stacking bilayer WS<sub>2</sub> with various biaxial strains. Insert figure is the magnified part in the purple circle.



**Fig.5** Integrated parameter N at CBM and VBM for AA and AB stacking bilayer WS<sub>2</sub> with different biaxial strain from  $-9.6\%$  to  $10\%$ . In cell figure is the difference between slopes of N<sub>CBM</sub> and N<sub>VBM</sub> curves.



**Fig.7** Band gap of AA and AB stacking bilayer WS<sub>2</sub> with various uniaxial strain  $\varepsilon$ , from  $-9.6\%$  to  $10\%$ . Similar tendency is observed. The band gap decreases with increasing tensile strain but increases first and then decreases with compressive strain.