# Non-negligible Metal Ions Diffusion in Amorphous Oxygen-Deficient Metal-Oxide Based Resistive Switches: A First Principle Study 

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#### Abstract

Taking amorphous $\mathrm{TaO}_{\mathrm{x}}$ and $\mathrm{HfO}_{\mathrm{y}}\left(\mathrm{a}-\mathrm{TaO}_{\mathrm{x}}\right.$ and $\left.\mathrm{a}-\mathrm{HfO}_{\mathrm{y}}\right)$ based resistive switches as examples, we perform systematic investigation on the ionic conductivities in $\mathrm{a}-\mathrm{TaO}_{\mathrm{x}}(\mathrm{x}=$ $2,1.5$ and 1 ) and $a-\mathrm{HfO}_{\mathrm{y}}(\mathrm{y}=1.5,1$ and 0.75$)$ from first principles. Our results reveal that the self-diffusion of O is predominant in both the $\mathrm{a}-\mathrm{TaO}_{\mathrm{x}}$ and $\mathrm{a}-\mathrm{HfO}_{\mathrm{y}}$ based resistive switches, and the diffusions of both O and metal (Ta or Hf ) ions become faster with the increase of O vacancy concentrations. The $\mathrm{O} / \mathrm{Ta}$ ionic conductivity in $\mathrm{a}-\mathrm{TaO}_{\mathrm{x}}$ is $3 \sim 5$ orders higher than that of $\mathrm{O} / \mathrm{Hf}$ in $\mathrm{a}-\mathrm{HfO}_{y}$ at the same O content. To our surprise, in the $\mathrm{a}-\mathrm{TaO}_{\mathrm{x}}$ with high O vacancy concentration (i.e., $x=1.5$ and 1 ), the diffusion of Ta becomes comparable to that of O in a wide range of temperature (from 300 K to 1673 K ). On the other hand, the diffusion of Hf in the $\mathrm{a}-\mathrm{HfO}_{\mathrm{y}}(\mathrm{y}=1$ and 0.75$)$ is 1 order smaller than that of O at 1673 K , and the diffusion coefficients ratio between Hf and O becomes gradually larger with the decrease of temperature. Based on these results, we propose that, in the low resistance state (or high O vacancy concentration), the diffusion of metal ions is non-negligible in metal-oxide based resistive switches, especially in the $a-\mathrm{TaO}_{x}$.


## 1. Introduction

O-deficient metal-oxide based resistive switching device has attracted considerable attention due to its high scalability, fast switching speed, low power consumption and potential application in next-generation resistive random access memories (RRAMs).[1] The resistive switch has a simple metal-insulator-metal (MIM) structure where an insulator $\left(\mathrm{HfO}_{\mathrm{x}},[2] \mathrm{ZrO}_{\mathrm{x}},[3] \mathrm{TaO}_{\mathrm{x}}\right.$, , 4$]$ and $\mathrm{NbO}_{\mathrm{x}}$ [5] etc.) layer is sandwiched between two electrically conductive electrodes. A pristine resistive switch with a high resistance state (HRS) can be switched into a low resistance state (LRS) by applying bias voltage, and the polarities of bias voltage in the SET (from HRS to LRS) and RESET (from LRS to HRS) operations of the switch are opposite to each other.

So far, amorphous $\mathrm{TaO}_{\mathrm{x}}\left(\mathrm{a}-\mathrm{TaO}_{\mathrm{x}}\right)$ and $\mathrm{HfO}_{\mathrm{y}}\left(\mathrm{a}-\mathrm{HfO}_{\mathrm{y}}\right)$ based resistive switches have been extensively reported in the literature, and show extremely high endurance, compared to RRAMs using other materials.[2,4] It is believed that the switching mechanism of resistive switches based on O-deficient materials can be ascribed to the drift/diffusion of O ions or vacancies driven by the electric field.[1] However, the role of metal ions diffusion has nev-
er been considered yet. In fact, several decades ago, Davies et al.[6] and Fehlner et al.[7] have found the diffusion of both metal and O species during the growth of oxide films such as in $\mathrm{Al}_{2} \mathrm{O}_{3}, \mathrm{Nb}_{2} \mathrm{O}_{5}$ and $\mathrm{Ta}_{2} \mathrm{O}_{5}$, though only O diffusion is observed in the cases of $\mathrm{HfO}_{2}, \mathrm{TiO}_{2}$ and $\mathrm{ZrO}_{2}$ at room temperature. In addition, the diffusion of Ta has been observed in $\mathrm{Ta} / \mathrm{SiOCH}$ interface, in which Ta atom is firstly oxidized into $\mathrm{TaO}_{\mathrm{x}}$, and then Ta ions could drift along with the applied electric field.[8] Thus, to deepen the understanding on the switching mechanism in O-deficient-materials (such as $a-\mathrm{TaO}_{x}$ and $\mathrm{a}-\mathrm{HfO}_{\mathrm{y}}$ ) based resistive switches, it is strongly desirable to examine the switching processes more closely, especially the contribution from the diffusion of metal ions. We take this by using first-principles calculations.

## 2. General Instructions

## Computational Methods

All calculations except those on transport properties were performed using the Vienna ab initio simulation package (VASP).[9] The model for amorphous $\mathrm{Ta}_{2} \mathrm{O}_{5}\left(\mathrm{a}-\mathrm{Ta}_{2} \mathrm{O}_{5}\right)$ was generated using the melt quenching method. The a- $\mathrm{Ta}_{2} \mathrm{O}_{5}$ model consists of 32 Ta and 80 O atoms, and the lattice constants are $\mathrm{a}=\mathrm{b}=14.68 \AA$, and $\mathrm{c}=8.19 \AA$. To generate the models for $\mathrm{a}-\mathrm{TaO}_{\mathrm{x}}(\mathrm{x}=2,1.5$ and 1$)$, the corresponding numbers of O atoms were removed randomly from the $\mathrm{a}-\mathrm{Ta}_{32} \mathrm{O}_{80}$, and melt quenching and subsequent relaxation (of both ionic position and cell volume) were performed. Similar procedure is also applied to generate amorphous $\mathrm{HfO}_{\mathrm{y}}\left(\mathrm{a}-\mathrm{HfO}_{\mathrm{y}}, \mathrm{y}=1.5,1\right.$ and 0.75) structures, where the a- $\mathrm{HfO}_{2}$ model consists of 36 Hf and 72 O atoms with the lattice constants $\mathrm{a}=\mathrm{b}=11.45 \AA$, and $\mathrm{c}=10.23 \AA$. For all the $\mathrm{a}-\mathrm{TaO}_{\mathrm{x}}$ and $\mathrm{a}-\mathrm{HfO}_{\mathrm{y}}$ structures, $2 \times 2 \times 4 k$-points were used during the optimization, and $4 \times 4 \times 8 k$-points were adopted for examining the electronic properties. The convergence criterion for the optimization was the maximum force acting on an atom to be smaller than $0.02 \mathrm{eV} / \AA$. Molecular dynamics (MD) simulation is carried out with the time step of 1 fs .

## Results and Discussion

To estimate the $\mathrm{O} / \mathrm{Ta}$ and $\mathrm{O} / \mathrm{Hf}$ diffusion in $\mathrm{a}-\mathrm{TaO}_{\mathrm{x}}(\mathrm{x}=2$, 1.5 and 1 ) and $a-\mathrm{HfO}_{y}(\mathrm{y}=1.5,1$ and 0.75$)$, we have generated time-average mean square displacement (MSD) plots at different temperatures, namely $873 \mathrm{~K}, 1073 \mathrm{~K}, 1273 \mathrm{~K}$, 1473 K and 1673 K . The time length ( 9 ps equilibration plus 30 ps MD run) employed for all temperatures considered is sufficient to observe the diffusive regime in the $a-\mathrm{TaO}_{\mathrm{x}}$ and
a- $\mathrm{HfO}_{\mathrm{y}}$. MSD increases linearly with time, and the increase in MSD also occurs with increase in temperature. The diffusion coefficient and activation energy can be extracted through a simple linear fitting scheme to the Arrhenius plot in Fig. 1 and 2.

Fig. 1 Computed diffusion coefficients of $a-\mathrm{TaO}_{x}$.


Fig. 2 Computed diffusion coefficients of $\mathrm{a}-\mathrm{HfO}_{\mathrm{x}}$.


It is found that both $\mathrm{O} / \mathrm{Ta}$ and $\mathrm{O} / \mathrm{Hf}$ diffusions are strongly related to the O stoichiometry in the suboxide: at a given temperature, the lower the O content, the faster the $\mathrm{O} / \mathrm{Ta}$ or $\mathrm{O} / \mathrm{Hf}$ diffusion. The calculated activation energies for O self-diffusion in $\mathrm{a}-\mathrm{TaO}_{\mathrm{x}}(\mathrm{x}=2,1.5$ and 1$), 0.59,0.41$ and 0.31 eV , respectively, decrease with the increase of the O vacancy concentrations. These results agree well with the experimentally estimated averaged activation energy for O atoms diffusion into $\mathrm{Ta} / \mathrm{Ta}$-suboxide, from 0.29 to 0.45 eV.[10] The estimated activation energies of O in $\mathrm{a}-\mathrm{HfO}_{\mathrm{y}}$ ( y $=1.5,1$ and 0.75 ) are within the range from 0.60 to 0.72 eV , which is slightly higher than those obtained by Clima et al. using bond-boosted ab initio MD simulation ( 0.57 to 0.66 eV , with $\mathrm{y}=1.97,1$ and 0.5 ).[11] Meanwhile, our calculated diffusion coefficient of O in $\mathrm{a}-\mathrm{HfO}_{\mathrm{y}}$ lies in the same range (from $10^{-12}$ to $10^{-9} \mathrm{~m}^{2} / \mathrm{s}$ ) as that of Clima et al. within the temperature from 873 to 1673 K . The activation energy of O diffusion in $\mathrm{a}-\mathrm{HfO}_{\mathrm{y}}$ is obvious higher than that in the case of $\mathrm{a}-\mathrm{TaO}_{\mathrm{x}}$, and the diffusion coefficient of O in $\mathrm{a}-\mathrm{HfO}_{\mathrm{x}}$ is $3 \sim 5$ orders lower than that in $\mathrm{a}-\mathrm{TaO}_{\mathrm{x}}$ at room temperature.

Interestingly, as the increase of O vacancy concentration, the diffusions of Ta and Hf become close to that of O as
shown in Fig. 1 and 2. For example, at room temperature, the diffusion coefficients of Ta in $\mathrm{a}-\mathrm{TaO}_{1.5}$ and $\mathrm{a}-\mathrm{TaO}$ are only 1 and 0.5 orders lower than those of O, respectively, and the diffusion coefficients of Hf in a-HfO and a- $\mathrm{HfO}_{0.75}$ are about 2 orders lower than that of O . Thus, for the $\mathrm{a}-\mathrm{TaO}_{\mathrm{x}}$ and $\mathrm{a}-\mathrm{HfO}_{\mathrm{y}}$ with high O vacancy concentration (i.e., $\mathrm{x} \leq 1.5, \mathrm{y} \leq 1$ ), the diffusion of metal ions is comparable to that of O , especially in $\mathrm{a}-\mathrm{TaO}_{\mathrm{x}}$.

## 3. Conclusions

Our results reveal that the diffusion of both O and metal ( Ta or Hf ) ions in $\mathrm{a}-\mathrm{TaO}_{\mathrm{x}}$ and $\mathrm{a}-\mathrm{HfO}_{\mathrm{y}}$ becomes faster with the increase of O vacancy concentrations. The $\mathrm{O} / \mathrm{Ta}$ ionic conductivity of $\mathrm{a}-\mathrm{TaO}_{\mathrm{x}}$ is obviously higher than that of $\mathrm{O} / \mathrm{Hf}$ in $\mathrm{a}-\mathrm{HfO}_{\mathrm{y}}$ at the same O content. At the high O vacancy concentrations (i.e., $x=1, y=0.75$ ), the diffusion coefficients of Ta and Hf are only $\sim 0.5$ and $\sim 2$ orders lower than that of O at room temperature, respectively. Thus, our results reveal that the diffusion of metal ions should be considered in explaining the switching mechanism of oxy-gen-deficient-materials based resistive switches, especially in $\mathrm{a}-\mathrm{TaO}_{\mathrm{x}}$.

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