

## Improvement of S-factor method for evaluation of MOS interface state density

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**Abstract** In this paper, the accuracy of the S-factor method for evaluating density of interface states ( $D_{it}$ ) at MOS interfaces is examined by simulation. Based on the analysis, we propose an improved S-factor method including the accurate depletion layer capacitance ( $C_d$ ), determined by gate-substrate capacitance ( $C_{gb}$ ) and gate-channel capacitance ( $C_{gc}$ ), and a new term in the analytical formulation of S factor. The accuracy of this method is also quantitatively studied.

**Introduction** Accurate interface state density ( $D_{it}$ ) evaluation of MOSFETs is still quite important, because the superior MOS gate stacks and reliability keep being a challenging issue for the advanced gates stacks and channels. Among a variety of the techniques, the S-factor method is taken as one of the simple and easy methods for evaluating  $D_{it}$  of MOSFETs [1]. Since the sub-threshold slope of  $I_d$ - $V_g$  curves of MOSFETs changes with the amount of  $D_{it}$ ,  $D_{it}$  in the weak inversion region can be extracted from the sub-threshold slope values, which is called the S-factor method [1-3]. However, to our best knowledge, the accuracy of  $D_{it}$  evaluated by the present S-factor method has not been examined yet.

In this paper, accuracy of the conventional S factor method is examined by using device simulation. Here, we provide two modifications to the S-factor method for higher accuracy of extracted  $D_{it}$  and obtaining  $D_{it}$  as a function of the surface potential ( $\phi_s$ ). One is more accurate determination of  $\phi_s$  by using  $C_d$  extracted from  $C_{gb}$  and  $C_{gc}$  and the other is to use more rigorous expression of the S factor by adding a new term. The correctness of  $D_{it}$  extracted by the modified method is quantitatively evaluated. Finally, experimental results of the energy distribution of  $D_{it}$  obtained by applying the present method to Si MOSFETs are shown.

**Experiment** Conventional Si nMOSFET with gate area  $100\ \mu\text{m} \times 100\ \mu\text{m}$  is used for device simulation as well as experiments. A constant mobility model is employed in the simulation.  $I_s$ -,  $C_{gb}$ - and  $C_{gc}$ - $V_g$  curves with and without  $D_{it}$  are simulated for nMOSFETs with different gate oxide thickness ( $T_{ox}$ ) and substrate impurity concentration ( $N_A$ ).

**Results and discussion** In the S factor method, as shown in Fig. 1, the slopes of  $\log_{10}I_s$ - $V_g$  curves in sub-threshold region, the S factor are used for  $D_{it}$  extraction. The analysis of the S factor is divided into two parts. The first part contains the evaluation of  $\phi_s$  under an equivalent capacitance model and the second part is related to the validity of the diffusion current model. As for the evaluation of  $\phi_s$ , a constant  $C_d$  value at  $\phi_s$  of  $1.5\phi_B$  is used, in the conventional S factor method [2, 3], under a series capacitance model of oxide capacitance ( $C_{ox}$ ) and  $C_d$  for obtaining average  $D_{it}$ . In order to obtain the energy distribution of  $D_{it}$ ,  $C_d$  must be determined as a function of  $V_g$  and  $\phi_s$ . Based on the equivalent circuit of the gate capacitance shown in Fig. 2,  $C_d$  can be determined as a function of  $V_g$  [4] by the equation of Fig. 2 using  $C_{gb}$  and  $C_{gc}$  curves, which can be experimentally measured, shown in Fig. 1. Fig. 3 shows the comparison between constant and extracted  $V_g$ -dependent  $C_d$ . The difference in  $C_d$  can lead to some error in  $D_{it}$  extraction. Fig. 4 shows the  $D_{it}$  values extracted from  $V_g$ -dependent  $C_d$  and constant  $C_d$  for simulations with constant  $D_{it}$  of  $5 \times 10^{11}\ \text{cm}^{-2}\text{eV}^{-1}$ . It is found that more accurate  $D_{it}$  is obtained for the present  $V_g$ -dependent  $C_d$  model. In order to check the accuracy of extracted  $C_d$  values, the present  $V_g$ -dependent  $C_d$  with

different  $T_{ox}$  are also compared with the direct expression of  $C_d$ , defined by  $dQ_s/d\phi_s$ , as shown in Fig. 5. Good agreement means the high accuracy of the present  $C_d$  extraction. In spite of the accurate  $C_d$  values, however, it is found that there are still remaining errors in  $D_{it}$  extraction. The energy distributions of  $D_{it}$  are obtained from the S factors by the conventional equation with the correction of  $C_{inv}$ , shown in Fig. 2, for MOSFETs without any  $D_{it}$ . Fig. 6 and 7 show the results with different  $T_{ox}$  and  $N_A$ , respectively. It is observed that  $D_{it}$  of meaningful orders, which is in a range of  $10^{10}$  to  $10^{11}\ \text{cm}^{-2}\text{eV}^{-1}$ , is inappropriately detected from interface-state-free MOSFETs, especially for thinner  $T_{ox}$  and lighter  $N_A$ . This fact suggests that the accuracy of any factors related to the diffusion current model is not sufficient.

The conventional analytical equation of the diffusion current in sub-threshold regions, which is a basis of the S factor method, is given in the inset of Fig. 8 [5]. In order to verify the accuracy of this expression, the S factors extracted from  $I_s$ - $V_g$  curves are compared between the simulated and the analytical calculations, as shown in Fig. 8. The good agreement guarantees the accuracy of the present analytical equation for diffusion current. It is found, on the other hand, that, when differentiating this equation with respect to  $\phi_s$ , a term proportional to  $S/\phi_s$  should be added to the conventional expression of  $D_{it}$ . The relationship between  $D_{it}$  and S including the new term is given by

$$D_{it} = \frac{1}{q} \left( \frac{qS}{kT \ln 10} - \frac{S}{2\phi_s \ln 10} - 1 \right) C_{ox} - \frac{C_d}{q} - \frac{C_{inv}}{q}$$

Fig. 9 and 10 show the energy distributions of  $D_{it}$  extracted by the new equation for MOSFETs without any  $D_{it}$  with different  $T_{ox}$  and  $N_A$ , respectively. Here, the vertical axis is taken as the absolute values of  $D_{it}$ , because the error component of  $D_{it}$  can be either positive or negative. It is found that, by taking the new term into account, the remaining error component of  $D_{it}$  becomes lower by around one order of the magnitude than that in Fig. 6 and 7. The minimum  $D_{it}$  is around  $2 \times 10^{10}\ \text{cm}^{-2}\text{eV}^{-1}$ , which can be the resolution limit of the present S-factor method. Also, the error component increases with increasing  $\phi_s$  toward the conduction band edge, attributable to the increase in the drift current component with an increase in  $\phi_s$ . Fig. 11 shows the energy distributions of  $D_{it}$  extracted from the improved S factor method for MOSFETs with  $1 \times 10^{11}$  and  $5 \times 10^{11}\ \text{cm}^{-2}\text{eV}^{-1}$ . The good agreement between extracted and assumed  $D_{it}$  values demonstrates the validity of the improved S factor method. Here, the energy range where the accurate extraction is realized seems to be from  $E_{mid} + 2kT$  to  $E_{inv} - 3kT$  and becomes wider for higher  $D_{it}$ . Fig. 12 shows the experimental energy distributions of  $D_{it}$  evaluated by the present method for Si nMOSFETs before and after FN stress to generate interface states. It is confirmed that  $D_{it}$  is successfully extracted down to lower half of  $10^{10}\ \text{cm}^{-2}\text{eV}^{-1}$  order as the minimum level.

**Conclusion** We have improved the S factor method in terms of the accuracy of  $D_{it}$  of MOSFETs by including  $V_g$ -dependent  $C_d$ , based on  $C_{gb}$  and  $C_{gc}$ , and the correction term for the analytical equation of the S factor, allowing us to obtain the energy distribution of  $D_{it}$ . It has been found that the accuracy of lower half of  $10^{10}\ \text{cm}^{-2}\text{eV}^{-1}$  order can be obtained for  $D_{it}$ .

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## References

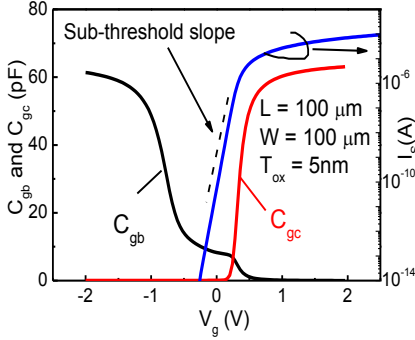
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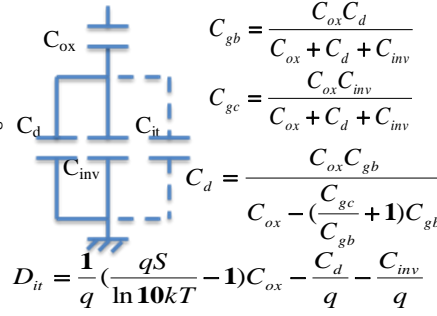
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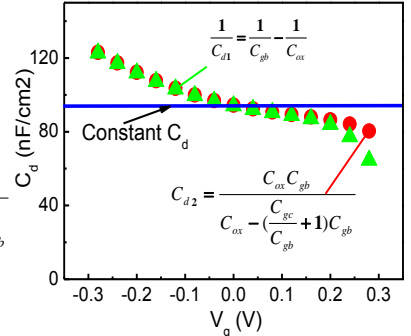
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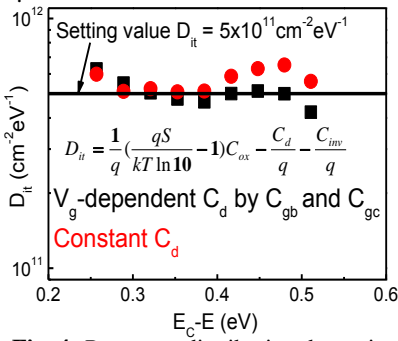
**Fig. 1**  $C_{gb}$ ,  $C_{gc}$  and  $I_s$ - $V_g$  curves in order to determine  $C_d$  and sub-threshold slope



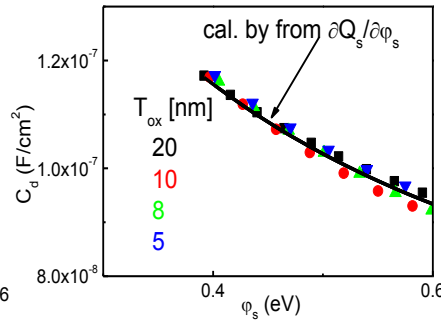
**Fig. 2** Equivalent circuit of MOS structure.



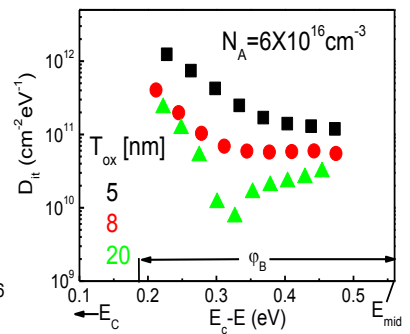
**Fig. 3**  $C_d$  from different extraction method.



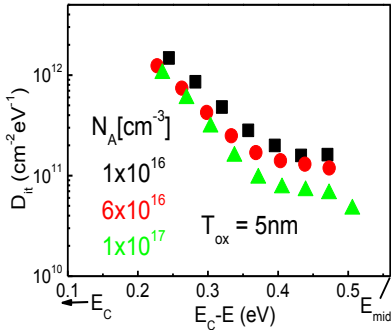
**Fig. 4**  $D_{it}$  energy distribution determined by constant  $C_d$  and  $V_g$ -dependent  $C_d$ .



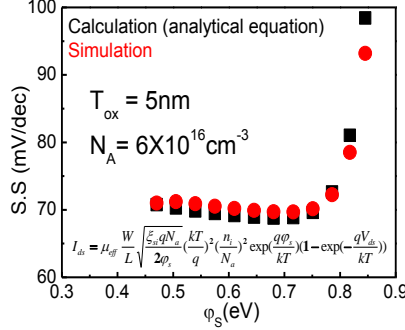
**Fig. 5** Comparison between simulation and analytical calculation result of  $C_d$ .



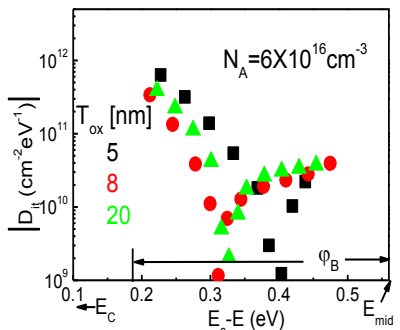
**Fig. 6**  $D_{it}$  extracted from S-factor method with different  $T_{ox}$  for the interface-state-free devices.



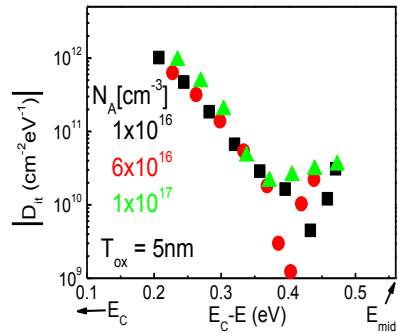
**Fig. 7**  $D_{it}$  extracted from S-factor method with different  $N_A$  for the interface-state-free devices.



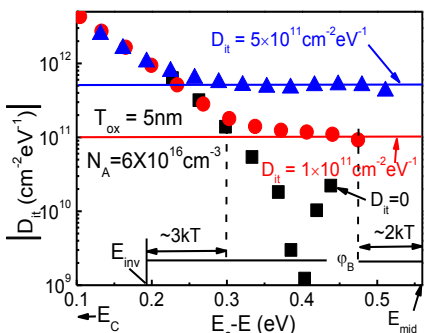
**Fig. 8** Comparison between simulation and analytical calculation result of S.S.



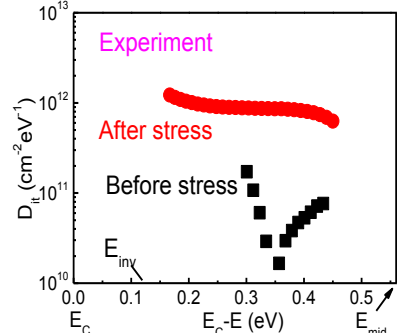
**Fig. 9**  $D_{it}$  extracted from S-factor method with different  $T_{ox}$  for the interface-state-free devices.



**Fig. 10**  $D_{it}$  extracted from S-factor method with different  $N_A$  for the interface-state-free devices.



**Fig. 11** Energy distribution of  $D_{it}$  for nMOSFET with given  $D_{it}$  values. Dotted line is the calculation result; Solid line is the  $D_{it}$  values used in the simulation.



**Fig. 12** Experimental result of  $D_{it}$  extracted by the improve S-factor method