# Minimization of Reverse Recovery Charge and Forward Voltage of Silicon pin Diodes

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## Abstract

The forward voltage  $V_{\rm f}$  and reverse recovery charge  $Q_{\rm rr}$  of silicon pin diodes are controlled by using the carrier lifetime or injection efficiency to reduce the power loss. In this study, the ideal lifetime and injection efficiency for minimizing the power loss is calculated by a theoretical analysis. The ideal lifetime has a current density dependency, and a decrease in the current density leads to an increase the ideal lifetime. Therefore, a shallow trap level indicates a smaller  $Q_{\rm rr}$  at the same  $V_{\rm fr}$ 

#### 1. Introduction

The forward voltage  $V_{\rm f}$  and reverse recovery charge  $Q_{\rm rr}$ of silicon pin diodes are proportional to the conduction and the turn-off loss, respectively [1]. In addition, they exhibit a trade-off relationship [1]. Therefore, it is a requirement to reduce  $V_{\rm f}$  and  $Q_{\rm rr}$ . To reduce the power loss, carrier lifetime control [2] or carrier injection efficiency control [3] can be used. In previous studies, we clarified that the power loss can be reduced by the appropriate choice of carrier control depending on dj/dt (rate of current density in turn off) [4].

In this study, we calculate the smallest  $V_{\rm f}$  and  $Q_{\rm rr}$  with the ideal carrier lifetime and carrier injection efficiency by theoretical analyses to minimize the total power loss.

# 2. Method

Figure 1 shows a diagram of the pin diode investigated in this study.  $N_p$ ,  $N_i$ , and  $N_n$  are the doping concentrations of the p, i, and n layers, and  $d_p$ , 2d, and  $d_n$  are the widths of the layers, respectively.  $C_i$  is the excess carrier density.

 $V_{\rm f}$  and  $Q_{\rm rr}$  can both be calculated from the excess carrier density distribution with the following equations [4]:

$$C_{i}(x) = \frac{J\eta_{i}\tau_{i}}{2qL_{ia}} \left\{ \frac{\cosh(x/L_{ia})}{\sinh(d/L_{ia})} - B' \frac{\sinh(x/L_{ia})}{\cosh(d/L_{ia})} \right\}$$
(1)

$$B' = \frac{1}{\eta_{\rm i}} \left( \frac{\mu_{\rm ie} / \mu_{\rm ih} - 1}{\mu_{\rm ie} / \mu_{\rm ih} + 1} + \eta_{\rm nh} - \eta_{\rm pe} \right)$$
(2)

$$V_{\rm f} = \frac{J}{q(\mu_{\rm ie} + \mu_{\rm ih})} \cdot \int \frac{1}{C_{\rm i}(x)} dx + \frac{kT}{q} \ln \left( \frac{C_{\rm i}(-d) \cdot C_{\rm i}(+d)}{n_{\rm i}^2} \right)$$
(3)

$$Q_{\rm r} = \frac{{\rm d} j}{{\rm d} t} \tau_{\rm i}^{\ 2} \ln^2 \left( \frac{\sqrt{Q_{\rm i}}}{\tau_{\rm i} \sqrt{{\rm d} j/{\rm d} t}} + 1 \right)$$
(4)

$$Q_{1} = \left(\eta_{i}\tau_{i}^{2}\frac{\mathrm{d}j}{\mathrm{d}t} + \tau_{i}J\eta_{i}\right)\left(1 - e^{-t_{i}/\tau_{i}}\right) - \frac{\mathrm{d}j}{\mathrm{d}t}\eta_{i}\tau_{i}t_{1} + Q_{0}e^{-t_{i}\tau_{i}}$$
(5)

$$t_1 = J / \frac{\mathrm{d} j}{\mathrm{d} t} \tag{6}$$

$$Q_0 = \int_{-d}^{+d} C_i(x) \mathrm{d}x \tag{7}$$



Fig. 1 Schematic of the pin diode with the doping distribution, excess carrier concentration, and current density.  $N_i = 5.0 \times 10^{13} / \text{cm}^3$ ,  $d_p = d_n = 3 \ \mu\text{m}$ , and  $2d = 140 \ \mu\text{m}$ .

where *J* is total current density,  $\eta_{pe}$ ,  $\eta_i$ , and  $\eta_{nh}$  is the ratio of the electron current density at the p/i, the recombination current density in the i layer, and the hole current density at the i/n, respectively,  $\tau_i$  is the carrier lifetime in the i layer,  $L_{ia}$  is the diffusion length in the i layer,  $\mu_{ie}$  and  $\mu_{ih}$  are the electron and hole mobilities in the i layer,  $n_i$  is the intrinsic carrier density.

 $\tau_i$  is determined by the Shockley–Read–Hall model [5]. Assuming a single energy level,  $\tau_i$  is expressed as

$$\frac{1}{\tau_{i}} = \frac{\sigma V_{ih} N_{i} Q_{0}}{2Q_{0} + 4dn_{i} \cosh\left(\frac{E_{i} - E_{i}}{kT}\right)} + \frac{1}{\tau_{i0}}$$
(8)

where  $\sigma$  is the capture cross section,  $v_{th}$  is the thermal velocity,  $N_t$  is the trap density, and  $\tau_{i0}$  is the intrinsic carrier lifetime in the bulk.  $E_t$  and  $E_i$  are the trap energy level of the trap and the midgap level.

## 3. Results and Discussion

Figure 2 shows the relationship between  $Q_{\rm rr}$  and  $\tau_{\rm i}$  for  $V_{\rm f} = 1.2$  V and J = 100 A/cm<sup>2</sup>. To maintain the same  $V_{\rm f}$ , the carrier injection efficiency is coordinated with  $\tau_{\rm i}$ . For the conditions in Fig. 2,  $Q_{\rm rr}$  achieves the minimum value around  $\tau_{\rm i} = 1.5$  µs. This  $Q_{\rm rr}$  is the smallest value when  $V_{\rm f} = 1.2$  V and J = 100 A/cm<sup>2</sup>.  $\tau_{\rm i}$  at the smallest  $Q_{\rm rr}$  is defined as the ideal lifetime  $\tau_{\rm ideal}$ .

The smallest  $Q_{\rm rr}$  can be determined for arbitrary values of  $V_{\rm f}$  and J. Figure 3 shows the relationship between  $V_{\rm f}$  and  $Q_{\rm rr}$  for various values of J. The ideal lines represent the smallest  $Q_{\rm rr}$  for any  $V_{\rm f}$  and J. The black points are the diode characteristics, which are controlled to have the smallest  $Q_{\rm rr}$ when  $V_{\rm f} = 2.0$  V and J = 200 A/cm<sup>2</sup> with various trap energy levels  $E_{\rm t} - E_{\rm i}$ . The current-density–voltage characteristics of these diodes are shown in Fig. 4.

At 200 A/cm<sup>2</sup>, any point lie on the ideal line. On the other hand, at 50 and 100 A/cm<sup>2</sup>, there is a difference between the points and the ideal lines. In addition, larger values of  $E_t - E_i$  are located closer to an ideal line. This is implies that shallow levels (large  $E_t - E_i$ ) are more suitable for achieving a reduced power loss.

Figure 5 shows the relationship between the lifetime and the current density for  $E_t - E_i = 0.0$  and 0.5 eV. The current-density dependency on the ideal lifetime is shown in same figure. Figure 5 indicates that a decrease in the current density leads to an increase in the ideal lifetime.



Fig. 2 The relationship between  $Q_{\rm rr}$  and  $\tau_{\rm i}$  for  $V_{\rm f} = 1.2$  V and J = 100 A/cm<sup>2</sup>.



Fig. 3 The relationship between  $V_{\rm f}$  and  $Q_{\rm rr}$  for various values of J.

From Eq. (8),  $\tau_i$  has same dependency on the stored charge at large values of  $E_t - E_i$ . Therefore,  $E_t - E_i = 0.5$  eV indicates more ideal characteristics in Fig. 3.

## 4. Conclusions

The smallest  $Q_{\rm rr}$  at the same  $V_{\rm f}$  with the ideal lifetime were calculated. The ideal lifetime has a current-density dependency, and a decrease in the current density leads to an increase in the ideal lifetime. Therefore, a shallow trap level (large  $E_{\rm t} - E_{\rm i}$ ) results in a smaller value of  $Q_{\rm rr}$ .

## References

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Fig. 4 Diode current–voltage characteristics for  $E_t - E_i = 0.0$ and 0.5 eV.



Fig. 5 The relationship between the lifetime and the current density for  $E_t - E_i = 0.0$  and 0.5 eV.