

## Determination of Dzyaloshinskii-Moriya Interaction Energy by Extended Droplet Model

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### Abstract

It has been known that lack of structural inversion symmetry with strong spin-orbit coupling at an interface of a ferromagnet (FM)/non-magnet (NM) bilayer generates the Dzyaloshinskii–Moriya interaction (DMI) which results in chirality in spin textures. Since chiral spin textures such as a skyrmion are an essential object for the next generation spintronics devices, it is important to determine DMI energy density ( $D$ ). In this study, we provide a simple method to estimate the  $D$  value using a conventional anomalous Hall effect (AHE) measurement.

### 1. Introduction

DMI between two atomic spins with an adjacent nonmagnetic atom having a strong spin-orbit coupling, is an essential mechanism in the FM/NM bi- (or multi-) layer system for developing state-of-the-art spin-orbitronic devices [1-3]. Recently, sub 100-nm-sized skyrmion-like bubble has been found to be a stable magnetic object with a sizable  $D$  [4-5]. Also, few hundreds m/s velocity of a Neel type domain wall (DW) arising from DMI is achievable [6]. Furthermore, DMI influences the current-driven switching and diode effect of the magnetic tunnel junction [7,8]. Therefore, it is important to determine the  $D$  value in FM/NM systems for realization of the next generation spintronic devices. In this presentation, we demonstrate how the DMI affects the magnetic domain nucleation under in-plane magnetic field ( $H_x$ ), which provides a simple way of estimating  $D$ .

### 2. Results and Discussions

For a magnetic droplet in a perpendicularly magnetized medium, a nucleation field ( $H_n$ ) is determined by the Zeeman energy and total DW energy ( $\sigma_{DW}$ ) of the magnetic droplet, thereby  $H_n = \sigma_{DW}^2$ . Here, we extend this droplet model as follows. The  $\sigma_{DW}$  with a single magnetization direction is given by [9];

$$\sigma_{DW}(H_x) = \begin{cases} \sigma_0 - \frac{\pi^2 \Delta M_S^2 \mu_0^2}{8K_D} (H_x + H_{DMI})^2, & \text{for } \mu_0 |H_x + H_{DMI}| \cdot \\ \sigma_0 + 2K_D \Delta - \pi \Delta M_S \mu_0 |H_x + H_{DMI}| & \text{otherwise,} \end{cases} \quad (1)$$

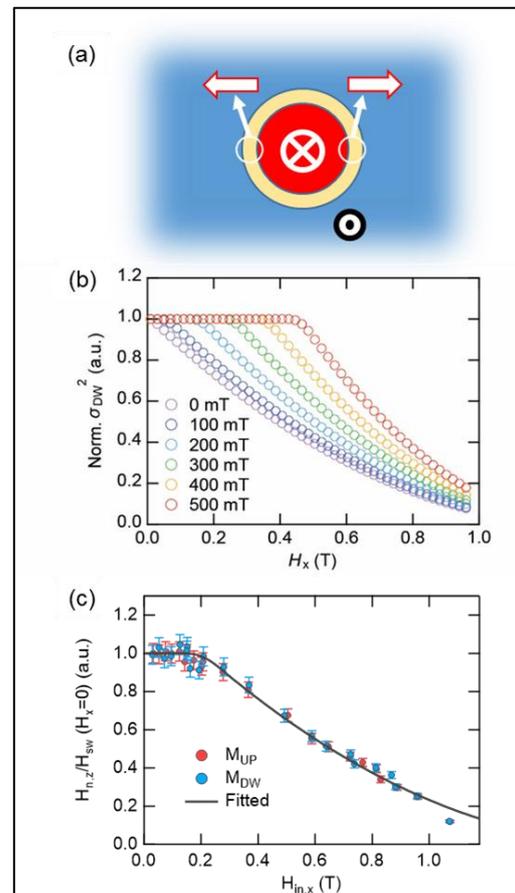


Figure 1. (a) A magnetic droplet with Néel DWs in a perpendicularly magnetized matter. (b) The normalized  $\sigma_{DW, total}^2$  as a function of  $H_x$ . (c) The normalized  $H_n$  vs.  $H_{in}$  curve of the Co/Ni multilayer on Pt.

where  $\sigma_0 (=4\sqrt{AK_{eff}})$  is the energy of a Bloch-type DW,  $A$  is the exchange stiffness constant,  $K_{eff}$  is the effective perpendicular anisotropy energy, and  $\Delta (= \sqrt{A/K_{eff}})$  is the DW width. When the DMI is stronger than DW anisotropy energy ( $K_D$ ), homochiral Néel type DWs are formed. Here, we assume that two DW magnetizations, parallel and antiparallel to  $H_{in}$ , dominate the  $\sigma_{DW}$  of the droplet [see red arrows in Fig. 1(a)]. As a result, the total  $\sigma_{DW}$  is given by

$\sigma_{\text{DW,total}}(|H_x|) = \sigma_{\text{DW1}}(+H_x) + \sigma_{\text{DW2}}(-H_x)$  because the left DW (DW1) and the right DW (DW2) are parallel and antiparallel to the direction of  $H_x$ , respectively. Figure 1 (b) is the normalized  $\sigma_{\text{DW,total}}^2$  vs.  $H_x$  curves in terms of  $H_{\text{DMI}}$ . Note that there is a critical field point. When the  $H_x$  is smaller than the critical field point,  $H_n$  does not depend on  $H_x$ . It is also clearly seen that the critical field is proportional to magnitude of  $H_{\text{DMI}}$ .

To prove the extended droplet model, we experimentally examined the  $H_n$  of the Co/Ni multilayer in terms of  $H_x$ . The  $H_n$  was estimated from the AHE signal. As predicted by the extended droplet model, the plot of  $H_n$  vs.  $H_x$  exhibits the critical point.  $H_{\text{DMI}}$  and  $D$  are confirmed to be  $228 \pm 60$  mT and  $0.45 \pm 0.15$  mJ/m<sup>2</sup>, respectively, from the best fitting.

Our model and simulation results are reproduced by the simulation. We calculate an energy barrier as a function of  $H_x$  and an out-of-plane field, based on the string method [10]. We find that the energy barrier varies significantly around a certain magnitude of  $H_x$ . This indicates that  $H_{\text{DMI}}$  is completely compensated in the  $x$  direction at the critical field strength. Therefore,  $H_{\text{DMI}}$  can be also calculated from the simulation. Finally, we estimate a DMI value of  $D \cong 0.45$  mJ/m<sup>2</sup> from the simulation result, which demonstrates the extended droplet model.

### 3. Conclusions

This study provide a simple model to describe the DMI effect on the nucleation of a perpendicularly magnetized droplet and a simple electrical measurement method to quantitatively determine the  $D$ , which is a key factor for next generation spin-orbitronic devices.

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